**Lecture 10**

Damping in Buildings

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The 21st Century Center of Excellence Program
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Damping

- **Reduction of intensity with time or spatial propagation**
  - Vibration Energy   Thermal Energy
  - Radiation to Outside

- **Cease of vibration with time**
- **Reduction of wind-induced/earthquake-induced vibration**
- **Increase of onset wind speed of aerodynamic instability**
- **etc.**

Damped Free Oscillation (Full-scale)

Damping Ratio = 0.93%

Amplitude (cm) vs Time (s)
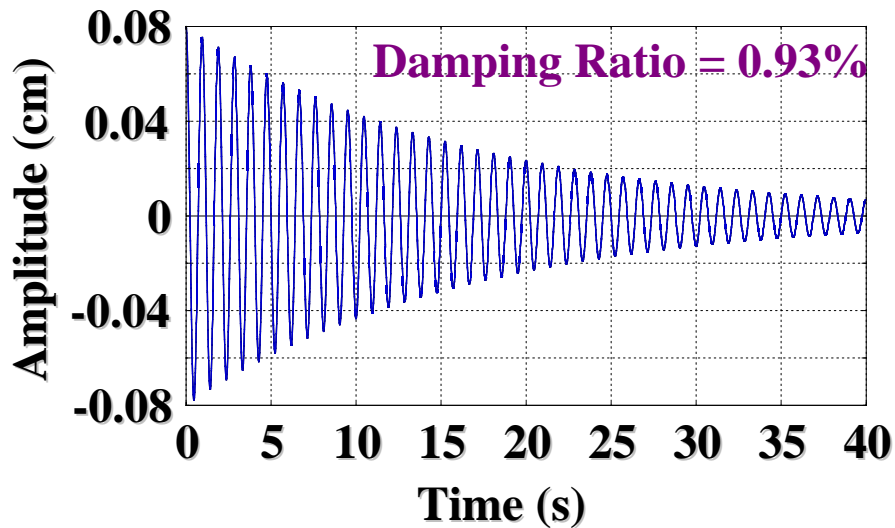
Damped Free Oscillation (SDOF)

$$x(t) = A\exp(-\zeta\omega_0 t)(\cos\sqrt{1-\zeta^2}\,\omega_0 t - \varphi)$$
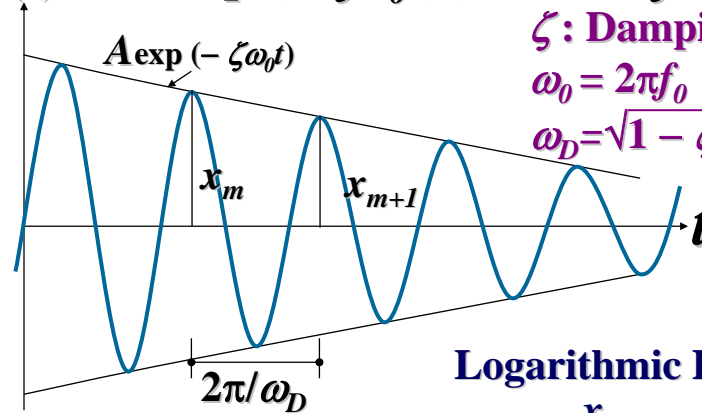
ζ : **Damping Ratio**

$\omega_0 = 2\pi f_0$

$\omega_D = \sqrt{1-\zeta^2}\,\omega_0 \approx \omega_0$

$A\exp(-\zeta\omega_0 t)$

x_m x_{m+1}

t

$2\pi/\omega_D$

Logarithmic Decrement

$$\delta = \ln\frac{x_m}{x_{m+1}} = \frac{2\pi\zeta}{\sqrt{1-\zeta^2}}$$

Damping in Buildings

- **Estimation of damping**
  - **no theoretical method**
  - **based on full-scale data**
       significant scatter

Dispersion of Damping Data

- Structural Materials
- Soil & Foundations
- Architectural Finishing
- Joints
- Non-structural Members
- Vibration Amplitude
- Non-stationarity of Excitations
- Vibration Measuring Methods
- Damping Evaluation Techniques
  etc.

Uncertainty of Response Prediction Due to Uncertainty of Damping Ratio

■ **Coefficient of variation of full-scale damping data**

ex. Havilland (1976)   C.O.V.   70%

If damping ratio was estimated at $\zeta = 2\%$ on average,

ζ *can generally take* **0.6%   3.4%** (2%± 1.4%

Wind-induced acceleration response

$A(\zeta = 0.6\%) \quad A(\zeta = 2\%) = \mathbf{1.8}$ ⎤ *2.3 times*
$A(\zeta = 3.4\%) \quad A(\zeta = 2\%) = \mathbf{0.8}$ ⎦

provides significant reduction of reliability of structural design

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Importance of Damping

■ **Improvement of Reliability of Structural Design**

Accurate **Response Prediction**
Accurate **Damping Predictor**
Reliable **Damping Database**

Physical Causes of Damping in Buildings

	Energy Dissipation Inside			Energy Dissipation Outside		
	Solid	Liquid	Gas	S–S	S–L	S–G
Friction	Internal Friction Damping	–		External Friction Damping	–	
Viscosity	–	Internal Viscous Damping		–	External Viscous Damping	
Radiation	–			Radiation Damping		–
Interaction	–			–	Hydro-dynamic Damping	Aero-dynamic Damping
Plasticity	Hysteretic Damping	–		–		

Internal Friction Damping

Energy dissipation due to internal friction of solid materials

- **Deformation of Materials**
  - Relative displacement between molecules
  - Slip of micro-cracks in microscopic structures such as crystals

Macroscopic: Elastic

Microscopic:
  - Friction damping between microscopic structures
    - Elastic hysteretic loss
    - Very small in metals (Energy loss ≈ 0.5%)

<< Different from energy loss due to plastic hysteresis>>

Plasticity Damping
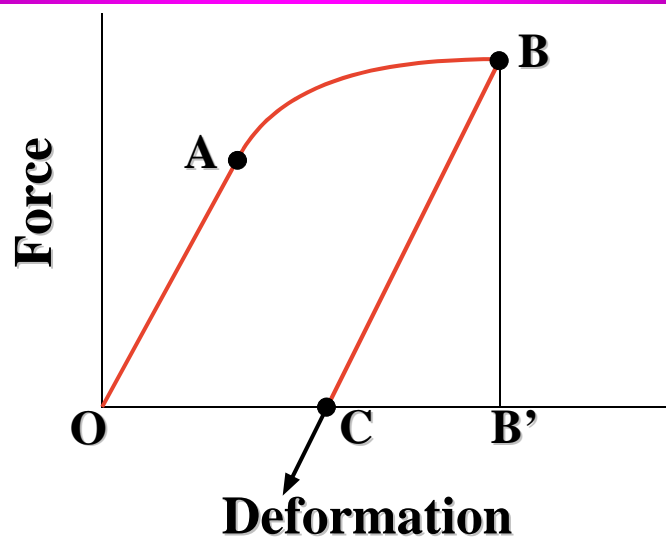
Energy dissipation due to plasticity of solids

- **Hysteresis due to Plasticity**

  Change in microscopic structure of materials

  Hysteretic characteristics / Plasticity Rate

Significantly greater than the energy dissipation due to internal material friction

Force-Deformation Relation of Structural Materials

Internal Viscous Damping

Energy dissipation due to internal viscosity of liquids

- **Molecular Viscosity**

  Collisions of molecules

  Coefficient of Kinetic Viscosity ν

  Conversion of kinetic energy to thermal energy

- **Turbulence Viscosity**

  Reynolds Stress (Virtual stress due to correlation of fluctuating velocity components of fluids)

  Coefficient of Kinetic Vortex Viscosity ν_t

  Mixture and diffusion of kinetic energy and so on

External Friction Damping

Energy dissipation due to friction between solids

- **Mainly Sliding Friction**
  Coefficient of Friction

  Work done by friction force preventing relative motion between solid bodies

  Conversion of vibration energy to thermal energy

  Sticking of molecules due to contact

  Damage and replacement of sticking due to relative motion

  Digging up by projections

  ex. Friction between joints, Friction between members, finishing etc.

Radiation Damping

Energy transfer between Solid – Solid, or Solid – Liquid

- **Propagation and loss of a system's energy to outside**
  - Necessary work for exciting a body contacting the system
  - Penetration of wave energy through boundary

  ex.
  - Radiation damping due to soil-structure interaction
  - Damping due to wave generation for a floating body

  Reflection of ground motions from building surface: Input loss

External Viscous Damping

Energy dissipation due to viscosity of liquids or gas contacting the body

- **Viscous resistance acting on a moving body in oil or water**

  - Large velocity gradient near body surface
  - A function of relative velocity

  ex.
  Oil Damper, Viscous Wall Damper

Fluid-Dynamic Damping
(Aerodynamic Damping)

Fluid-body interaction

- **Effects of relative velocity**
- **Effects of additional unsteady flow induced by body motion (Feedback system)**

 Ex.

 Along-wind Vibrations (Buffeting) due to turbulence:
 Positive Damping

 Across-wind Vibrations (Galloping, Vortex-resonance etc.): **Negative Damping**

Damping and Building Vibration

Careful and precise observation of **Vibration Phenomena**

Analytical Model with high accuracy

Damping Evaluation appropriate for the model

Equivalent Model, Mathematical Formula

Treatment of Damping   Restriction in numerical analysis

Soil-Structure Dynamic Interaction
Ground Domain   Boundary Treatment,
Internal Damping of Ground

Evaluation of higher mode damping Damping Matrix,

Value of Damping Ratio, Non-linear Range

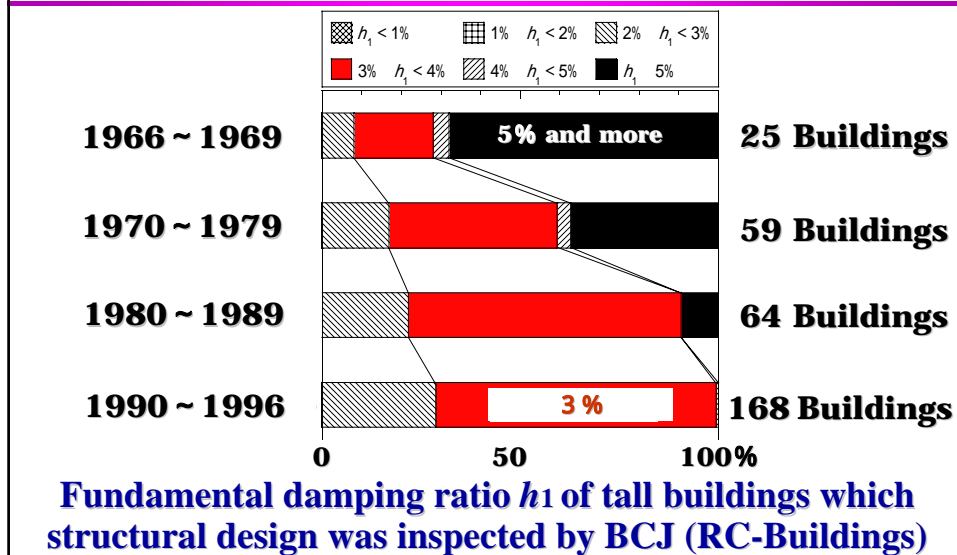# Damping Ratio of Buildings

- Damping Matrix Proportional to Stiffness Matrix
- Realistic Proportional Matrix Meeting Conditions
- Actual Damping Ratio
- Design Damping Ratio Closely Following Actual Phenomena
- Variation of Natural Frequency and Damping Ratio With Amplitude / Effects of Secondary Members
- Initial Stiffness / Instantaneous Stiffness
- Q-Δ and Damping Characteristics in Inelastic Range During Extremely Strong Earthquake
- Damping in Above Ground Structure / Soil-Structure Interaction / Full-scale Values of Damping Ratio
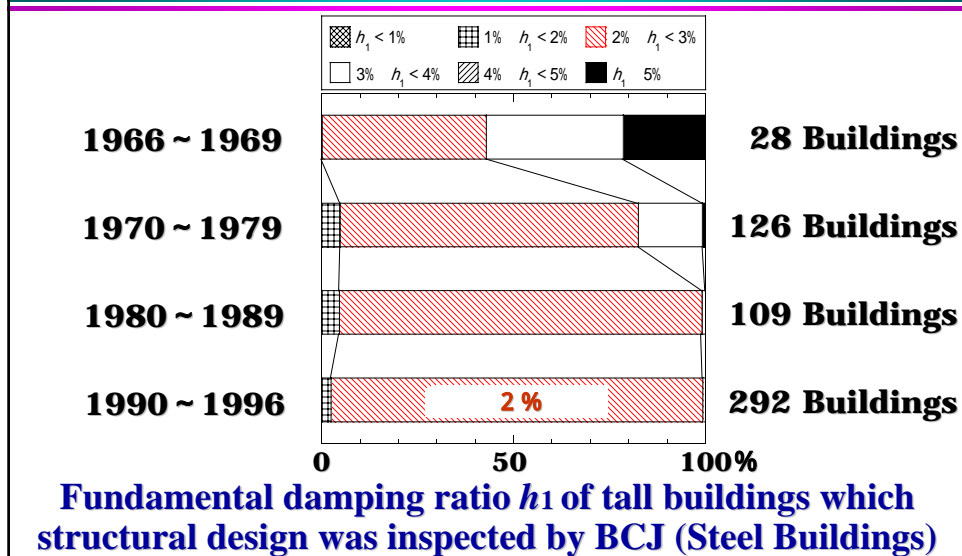- Damping for Vertical Vibrations ?

Currently Used Design Damping Values

- AS 1170.2 Part 2   - Chinese Standards
- DIN1055, Teil 4   - ESDU 83009
- EUROCODE 1   - ISO4354
- ISO/CD 3010   - ONORM B4014
- Swedish Code
- US Atomic Energy Commission   etc.

Design Damping Ratio Used in Japan

▨ h_1 1%	⊞ 1% h_1 2%	◫ 2% h_1 3%
🟥 3% h_1 4%	▨ 4% h_1 5%	⬛ h_1 5%

1966 1969	5 and more	**25 Buildings**
1970 1979		**59 Buildings**
1980 1989		**64 Buildings**
1990 1996		**168 Buildings**

0 50 100

Fundamental damping ratio h_1 of tall buildings which structural design was inspected by BCJ (RC-Buildings)

Design Damping Ratio Used in Japan

▨ h_1 1%	⊞ 1% h_1 2%	▨ 2% h_1 3%
☐ 3% h_1 4%	▨ 4% h_1 5%	⬛ h_1 5%

1966 1969		**28 Buildings**
1970 1979		**126 Buildings**
1980 1989		**109 Buildings**
1990 1996		**292 Buildings**

0 50 100

Fundamental damping ratio h_1 of tall buildings which structural design was inspected by BCJ (Steel Buildings)

11

Currently Used Damping Values
(Steel Buildings)

Country	Actions/Stress Levels	Joints/Structures	Damping ratios ζ_1 (%)
Australia	Serviceability		0.5 – 1.0
(AS1170.2)	Ultimate & Permissible	Frame Bolted	5
		Frame Welded	2
Austria	(ÖNORM B4014)		
China	(GB50191-93)	Steel (TV) Tower	2
France		Standard Bolt	0.8
		High Resistance Bolt	0.5
		Welded	0.3
	Earthquake	Bolt	4
		Welded	2
Germany	Wind (DIN 1055)		
Italy	Wind (EUROCODE 1)		
	Earthquake		5
Japan	Habitability		1
	Earthquake		2
Singapore			1
Sweden	(Swedish Code of Practice)		0.9
United Kingdom	Wind (ESDU)		
USA (Penzien, US Atomic Energy Commission)			

Currently Used Damping Values
(RC Buildings)

Country	Actions/Stress Levels	Structures	Damping ratios ζ_1 (%)
Australia	Serviceability	RC or Prestressed C	0.5 – 1.0
(AS1170.2)	Ultimate & Permissible	RC or Prestressed C	5
Austria	(ÖNORM B4014)		
China	(GB50191-93)	RC Structures	5
		RC (TV) Towers	5
		Prestressed RC Tower	3
France		Standard	1.6
		Reinforced	0.65
	Earthquake	Standard	3 - 4
		Reinforced	2
Germany	Wind (DIN 1055)		
Italy	Wind (EUROCODE 1)		
	Earthquake		5
Japan	Habitability		1
	Earthquake		3
Singapore			2
Sweden	(Swedish Code of Practice)		1.4
United Kingdom	Wind (ESDU)		
USA	(US Atomic Energy Commission)		

DIN 1055
Teil 4, The German Pre-Standard

Wind (Actual Wind Load Code)

Structures	Conditions	Damping ratios ζ_1 (%)
- Steel	Bolted	0.5 – 0.8
	Welded	0.3
- Reinforced C	Without cracks	0.6
	With cracks	1.6
- Prestressed C		0.6

ESDU
Damping of Structures – Part 1
Tall Buildings, 83009, 1983

Wind

- **1st mode damping ratio ζ_1 (%)**

$$\zeta_1 = \zeta_s + \zeta_a$$

ζ_s : Structural damping ratio

$$\zeta_s = 100\left(\zeta_{s0} + \zeta' \frac{x_H}{H}\right) \leq \frac{60}{H} + 1.3 \quad (\%)$$

$\zeta_{s0} = f_1 / 100$ (Most Probable), $f_1/250$ (Lower Limit)

$\zeta' = 10^{\sqrt{D}/2}$ (Most Probable), $10^{\sqrt{D}/2.5}$ (Lower Limit)

ζ_a : Aerodynamic damping ratio

x_H : Tip displacement (m), H : Building height (m)

f_1 : 1st mode natural frequency (Hz)

EUROCODE
Wind Actions, ENV-1991, 1994

Wind

- **1st mode damping ratio ζ_1 (%)**

$$\zeta_1 = \zeta_s + \zeta_a + \zeta_d$$

ζ_s : **Structural damping ratio**

$\zeta_s = a\,f_1 + b \geq \zeta_{min}$

$f_1 = 46\,/\,H$ (1st mode natural frequency)
$a =$ 0.72 (Steel),   0.72(RC)
$b =$ 0   (Steel),   0.8 (RC)
$\zeta_{min} = 0.8$ (Steel),   1.6 (RC)

ζ_a : **Aerodynamic damping ratio**

ζ_d : **Damping ratio due to vibration control devices**

ÖNORM B4014
Teil 1, Code for Austria

Wind (Actual Wind Load Code for Austria)

- **1st mode damping ratio ζ_1 (%)**

$$\zeta_1 = \zeta_m + \zeta_c + \zeta_f$$

ζ_m : **Structural damping ratio** due to materials (%)
0.08 (Steel)
0.72 (RC with cracks), 0.4 (RC without cracks, PSRC)

ζ_c : **Structural damping ratio** due to constructions (%)
0.32 (Steel tall buildings),
0.32 (RC tall buildings, Panel systems)
0.64 (RC tall buildings, Frame systems)

ζ_f : **Structural damping ratio** due to foundations (%)
0.08 (Support with hinges)
0.24 (Support with sliding bearings)
0.16 (Fixed support of frame structures)
etc.

US Atomic Energy Commission
"Regulatory Guide"

Structures	Damping Ratio (%)	
	OBE or ½ SSE	SSE
Welded Steel	2	4
Bolted Steel	4	7
Prestressed C	2	5
Reinforced C	4	7

OBE : Operating Basis Earthquake
**SSE : Safe Shutdown Earthquake**

ISO

- **ISO4354** (Wind Actions on Structures, 1997)
  1st mode damping ratio
  $\zeta_1 = 1.0\ \%$ (Steel Buildings)
  $\zeta_1 = 1.5\ \%$ (RC Buildings)

- **ISO/CD3010** (Seismic Actions on Structures, 1999)
  1st mode damping ratio
  $\zeta_1 = 2 - 5\ \%$

Design Damping Ratios Currently Used in Various Countries (Steel Buildings)
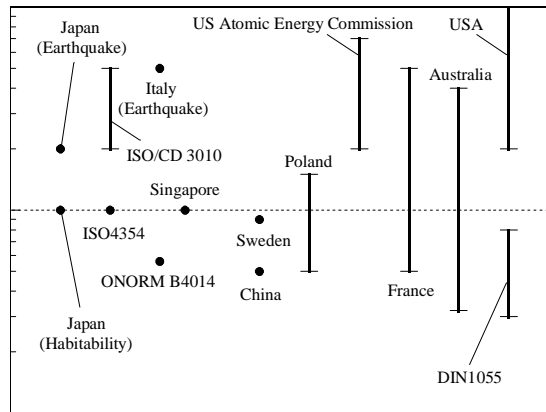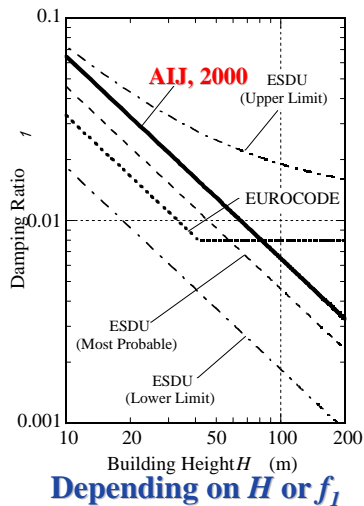
Depending on H or f_1

For All Buildings: Depending on Connection Types, Stress Levels, Foundation Types, etc.

Design Damping Ratios Currently Used in Various Countries (RC Buildings)
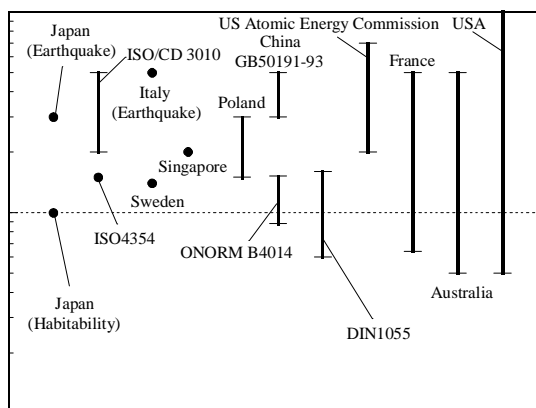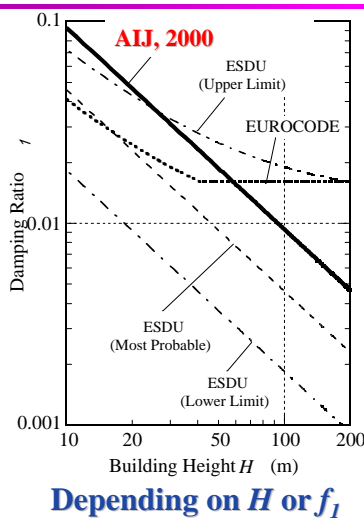
Depending on H or f_1

For All Buildings: Depending on Concrete Materials, Stress levels, Foundation Types, etc.

Damping Data & Predictors

- **Penzen, J. (1972), U.C. Berkley**
- **Haviland, R. (1976), MIT**
- **Cook, N.J. (1985) 'The designer's guide to wind loading of building structures'**
- **Davenport, A.G. & Hill-Carrol, p. (1986), ASCE**
- **Jeary, A.P. (1986), *JEESD***
- **Lagomarsino, S. (1993), *JWEIA***
- **Ellis, B.R. (1998)**
- ***etc.***

Desirable Damping Database

- **Enough Data**
- **Enough Building Types**
- **High-Quality & Accurate**
- **Information in Detail**
  - **Building & Soil**
  - **Measuring Conditions**
  - **Evaluation Techniques**
  - **Amplitudes**
  - **Stationarity**

Japanese Damping Database

Research Committee on Damping Data
organized by
**Architectural Institute of Japan
(1993-2000)**

Sources of Damping Data

- Original data from Members of the Research Committee
- Research Committee Report on Evaluation of Damping of Buildings, Building Center of Japan, 1993
- Summary Papers presented at the *Annual Meeting of Architectural Institute of Japan* (AIJ) 1970 -
- *Journal of Structural and Construction Engineering* (Transactions of AIJ), 1970 -
- Proc. *Annual Meeting of Kanto Branch of Architectural Institute of Japan*, 1970 -
- Proceedings of *Annual Meeting of Kinki Branch of Architectural Institute of Japan*, 1970-
- Proc. *National Symposium on Wind Engineering*, 1970 -
- Proc. *National Symposium on Earthquake Engineering*, 1970 -
- Proc. *International Conference on Earthquake Engineering*, 1974 -
- Vibration Tests of Buildings, *Architectural Institute of Japan*, 1978
- Technical Reports published by *Research Institute of Construction Companies*, 1974 -

Accuracy and Quality of Damping Data

Questionnaire Studies to Designers and Owners

- **Confirmation of Values**
  - Dynamic Properties in Literature
- **Collection of Necessary Data**
  - Building Information
  - Measurement Methods
  - Evaluation Techniques
  - Amplitudes
- **Exclusion of Unreliable Data**
- **Approval for World-Wide Distribution**

☞ *Many original non-published data and additional information were collected.*

Japanese Damping Database

(Damping in buildings, AIJ, 2000)

Number of Buildings and Structures			
285			
Steel Buildings (Steel)	Steel Encased Reinforced Concrete Buildings (SRC)	Reinforced Concrete Buildings (RC)	Tower-Like Non-Building Structures
137	43	25	80
$H_{Ave.}$= 101m	$H_{Ave.}$= 60m		$H_{Ave.}$= 124m
15.5m 282.3m	11.6m 167.4m	10.8m 129.8m	9.1m 226.0m
Office : 99 Hotel : 25 Others : 13	Apartment : 35 Office : 20 School : 4 Others : 9		Chimney : 26 Lattice : 24 Tower : 23 Others : 6

19

Japanese Damping Database (JDD)

(Damping in buildings, AIJ, 2000)

	Contained Information	
Building Information	Location Time of Completion Building Usage Shape Height Dimensions Number of Stories	Structural Type Cladding Type Foundation Type Embedment Depth Length of Foundation Piles Soil Conditions Reference
Dynamic Properties	**Damping Ratio** **(up to the 6th mode)** **Natural Frequency** **(up to the 6th mode)** Time of Measurement	Excitation Type Experimental & Measurement Method Evaluation Technique Amplitude etc.

Fundamental Natural Period (JDD)
(Steel Buildings)

(Damping in buildings, AIJ, 2000)

$$T_1 = 0.020H, \quad r = 0.94$$

Figure: Natural Period T_1 (s) versus Building Height H (m)
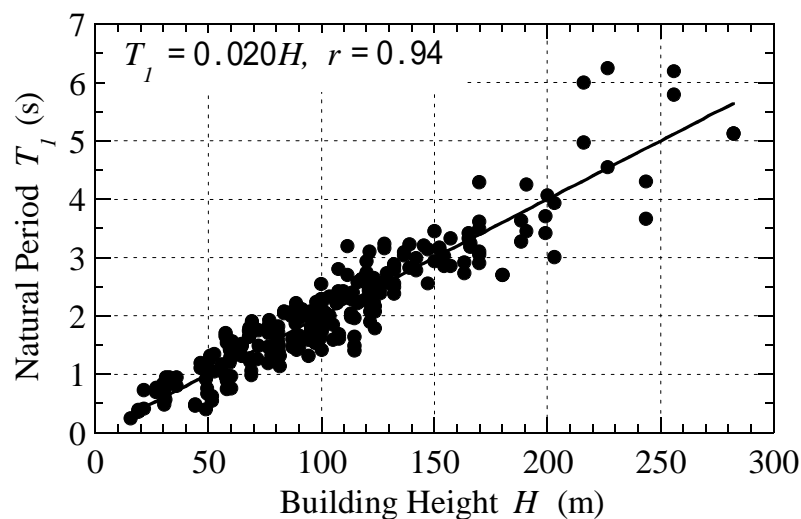
Fundamental Natural Period[(JDD)] (RC/SRC Buildings)

(Damping in buildings, AIJ, 2000)
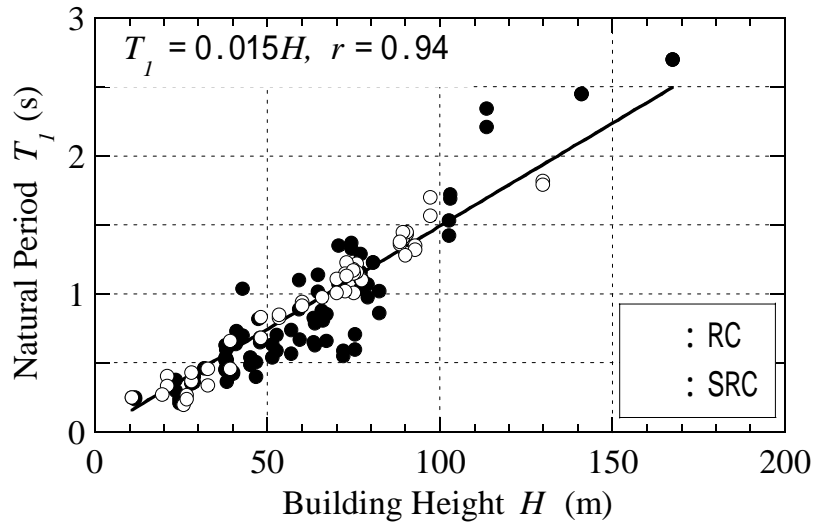
Higher Translational Mode [(JDD)] Natural Periods (Steel Buildings)

(Damping in buildings, AIJ, 2000)
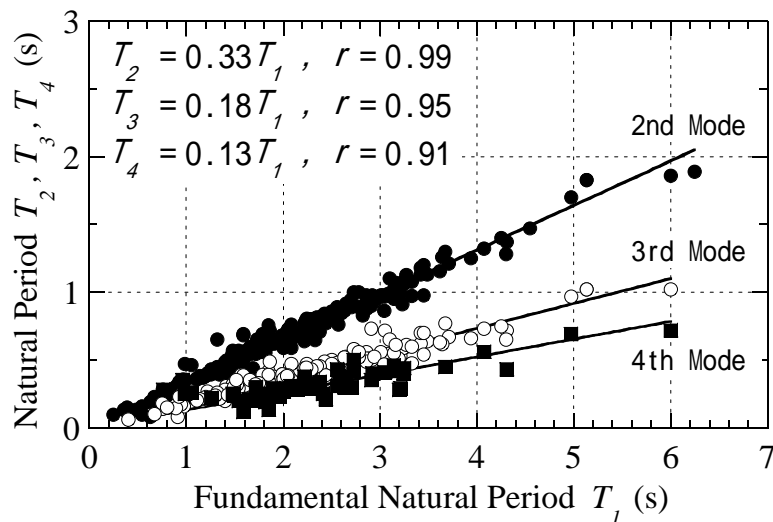
Torsional Mode Natural Periods (JDD)

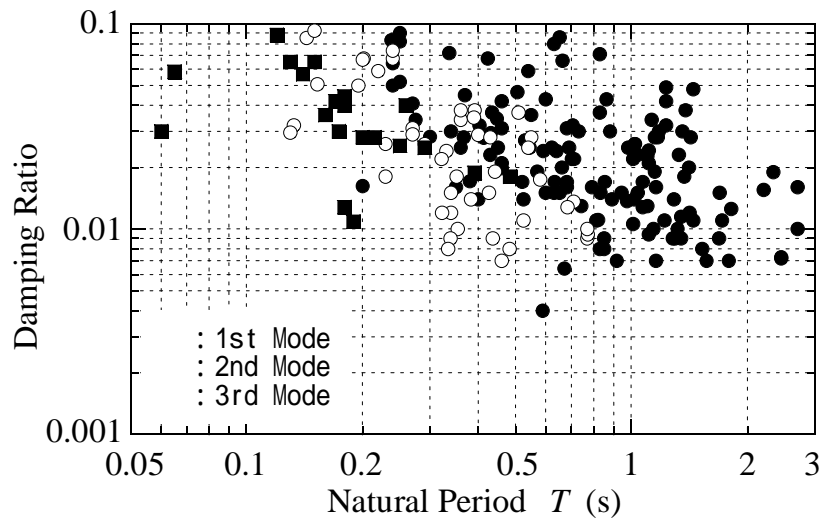**(Damping in buildings, AIJ, 2000)**
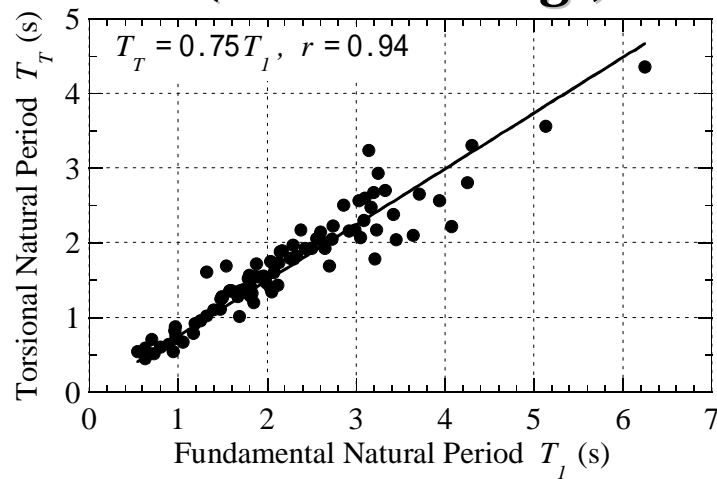
(Steel Buildings)

$$T_T = 0.75 T_1, \quad r = 0.94$$

Torsional Natural Period T_T (s) vs Fundamental Natural Period T_1 (s)

Damping Ratios & Natural Periods (Steel Buildings)

(Damping in buildings, AIJ, 2000)

135 Steel Buildings

Translational Damping Ratio ζ (%) vs Translational Natural Period T (sec)

- ● 1st
- ■ 2nd
- ▨ 3rd
- ▲ 4th
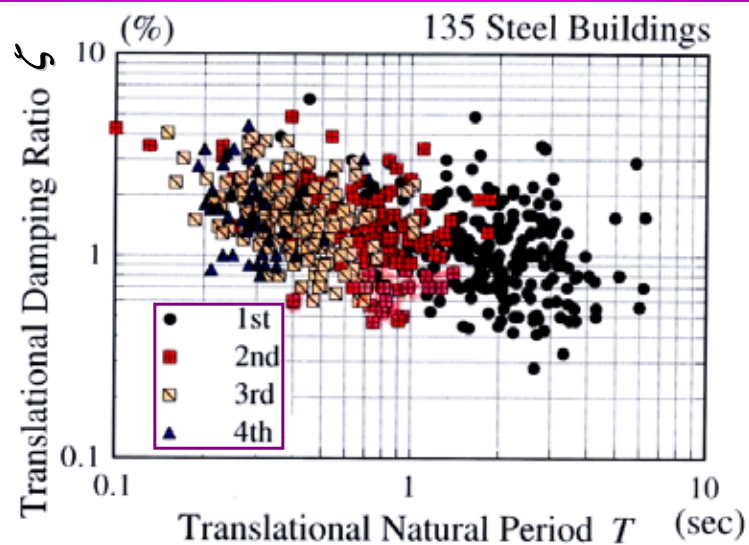
Damping Ratios & Natural Periods
(RC/SRC Buildings)

Damping Predictors

- **Jeary (1986) :**
$$\zeta_1 = 0.01f_1 + 10^{\sqrt{D/2}}(x_H/H)$$
- **Lagomarsino (1993) :**
$$\zeta_1 = \alpha/f_1 + \beta f_1 + \gamma(x_H/H)$$

D : Building Dimension along Vibration Direction

x_H/H : Tip Drift Ratio

Jeary's Damping Predictor

$$\zeta_1 = \zeta_0 + \zeta_I \ x/H$$
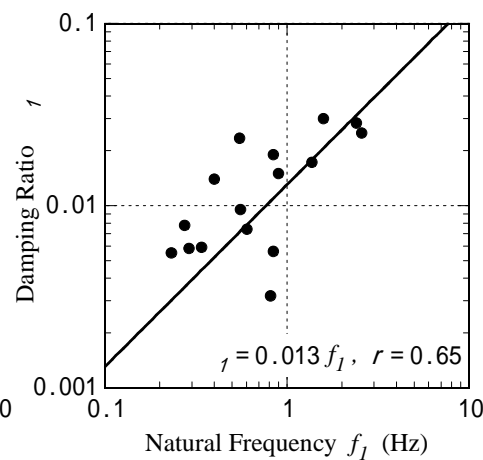
$$\zeta_0 = f_1/100$$
$$\zeta_I = 10^{\sqrt{D}/2}$$

All joints and contact surfaces slip

High amplitude plateau region

ζ_I

Friction between elements

Small low amplitude plateau region with ζ_0

ζ_0

ζ
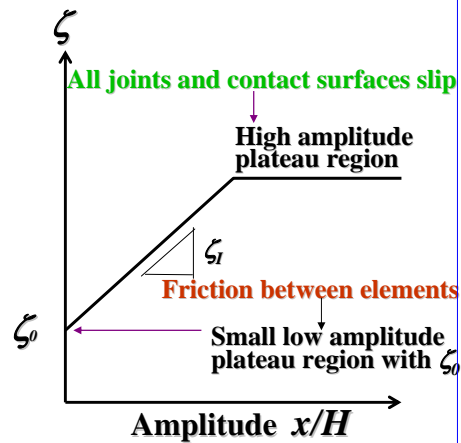
Amplitude x/H

f_1 **Lowest Natural Frequency (Hz)**

D **Width of Building Base in Vibration Direction (m)**

Fundamental Damping Ratios for Very Low-Amplitude Data

Damping Ratio ζ_1

$\zeta_1 = 0.014 f_1$, $r = 0.89$

Natural Frequency f_1 (Hz)

RC Buildings

$\zeta_1 = 0.013 f_1$, $r = 0.65$

Natural Frequency f_1 (Hz)

Steel Buildings

Very Low-Amplitude Data

● **Frequency Dependent Term**
  RC buildings :
  $$\zeta_1 = 0.0143\, f_1 \qquad (\, r = 0.89)$$
  SRC buildings :
  $$\zeta_1 = 0.0231\, f_1 \qquad (\, r = 0.32)$$
  Steel buildings :
  $$\zeta_1 = 0.013\, f_1 \qquad (\, r = 0.65)$$
  f_1: **Fundamental Natural Frequency (Hz)**

Variation of Damping Ratio with Amplitude

H=100m Steel Building (Jeary,1998)

Damping Ratio (%) vs Tip Displacement (mm)

Stick-slip Model
for Damping in Buildings

Q

Q_c

k

1

0   x_c x

Stick

X

k

← Friction

$Q = kx < Q_c$

Slip

X

X_c

k

← Friction

$Q = Q_c$
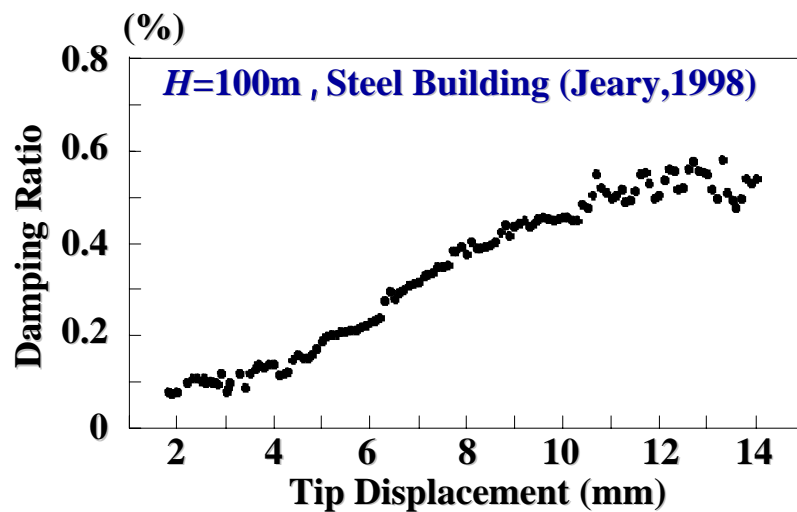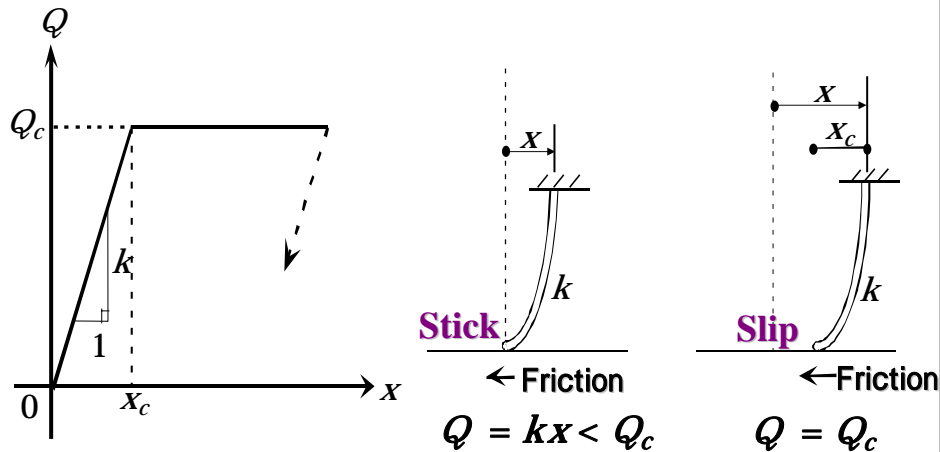
Stick-slip Model
for Damping in Buildings

Increase of amplitude
→ **Increase of number of slipping joints**
→ **Increase of friction damping**
　& Decrease of stiffness
　Sum of a lot of frictional damping effects
　≈ Viscous damping

+ ⋯ + ⋯⋯⋯⋯ =
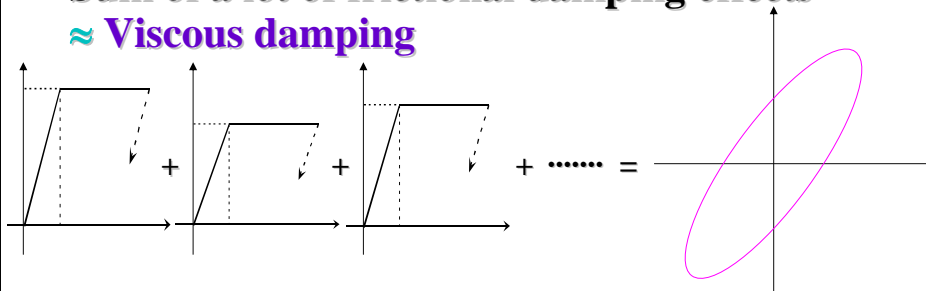
An Observatory Building (H=99m)
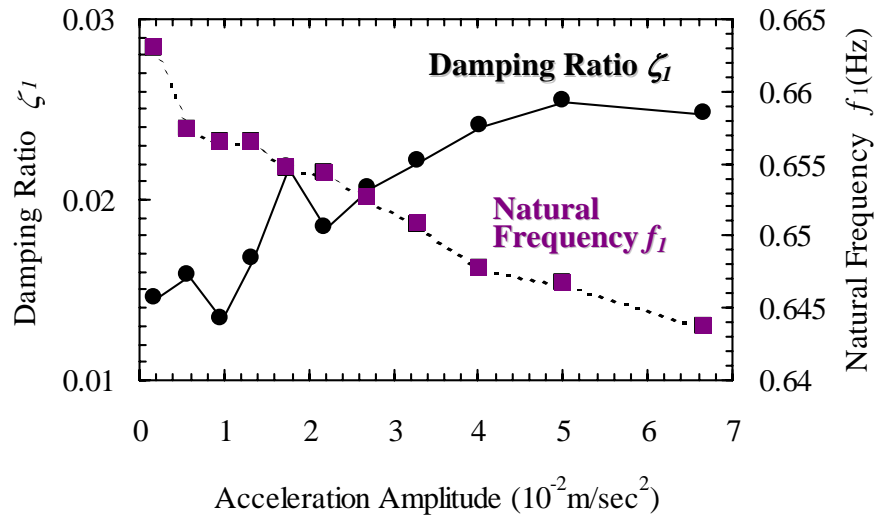
Amplitude Dependence of Damping Ratio

(Damping in buildings, AIJ, 2000)

■ **Steel Buildings**

$$\zeta_1 = B \frac{x_H}{H}$$

Tall Office Buildings :
$B = 400,$ Upper Limit $x_H / H = 2 \times 10^{-5}$
$\Delta\zeta_1 (x_H / H) = 0.8\%$

Tall Towers :
$B = 3000,$ Upper Limit $x_H / H = 5 \times 10^{-6}$
$\Delta\zeta_1 (x_H / H) = 1.5\%$

Proposed Damping Predictor in AIJ 2000

Natural Frequency Dependent Term
←**Height Dependent**
←**Soil-Structure-Interaction**

■ **RC buildings :**

$$\zeta_1 = 0.0143 f_1 + 470(x_H/H) - 0.0018$$

$$x_H/H < 2\times10^{-5}, \quad 30\text{m} < H < 100\text{m}$$

Large in Low-rise Buildings←

■ **Steel buildings :**

$$\zeta_1 = 0.013 f_1 + 400(x_H/H) + 0.0029$$

$$x_H/H < 2\times10^{-5}, \quad 30\text{m} < H < 200\text{m}$$

Comparison of Full-Scale Damping Ratios and Proposed Predictors

RC Buildings

Including Amplitude Dependent Term

Lagomarsino

AIJ 2000 **Frequency Dependent Term Only**
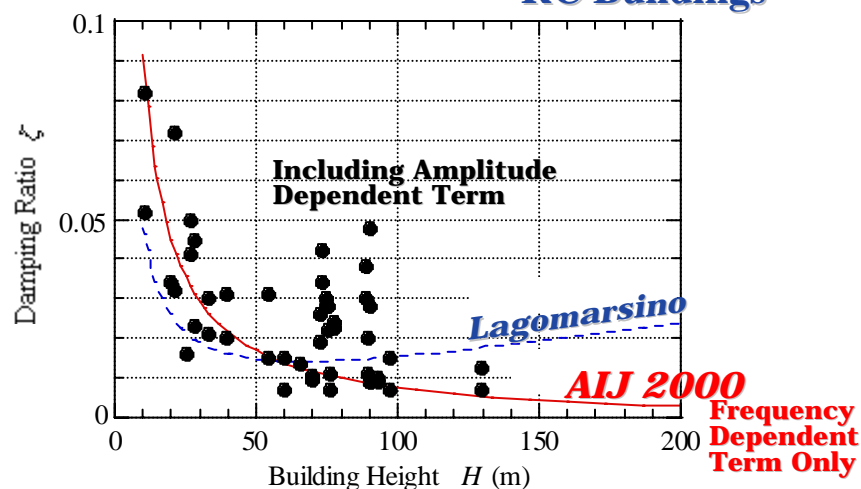
Comparisons of Full-Scale Damping Ratios and Proposed Predictors

Steel Buildings

Including Amplitude Dependent Term

Lagomarsino

AIJ 2000
Frequency Dependent Term Only

Eq.(12)(Proposal)

Damping Ratio ζ vs Building Height H (m)
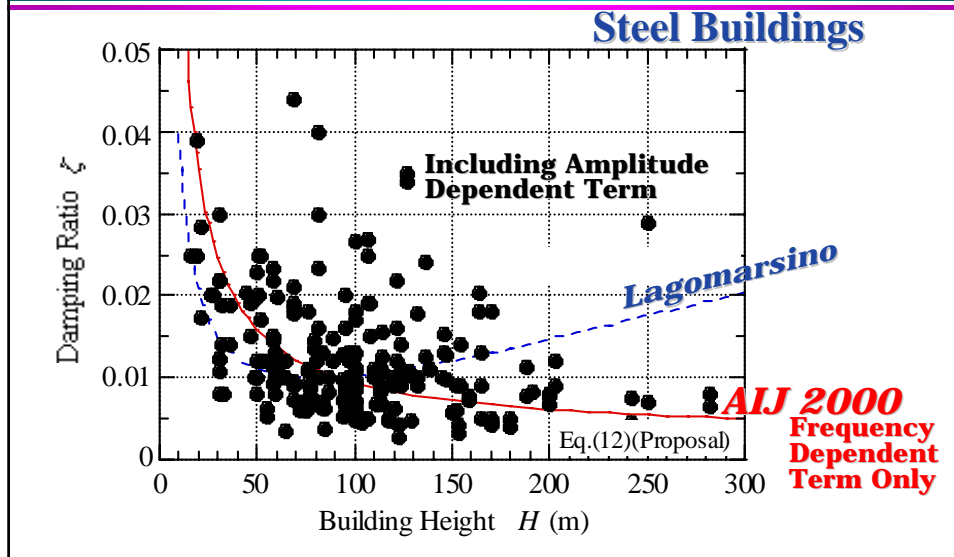
Full-Scale Known Amplitude Damping Ratios vs Proposed Predictor in AIJ 2000

RC Buildings

$r = 0.88$

Full-Scale Damping Ratio vs Predicted Damping Ratio by **AIJ 2000**
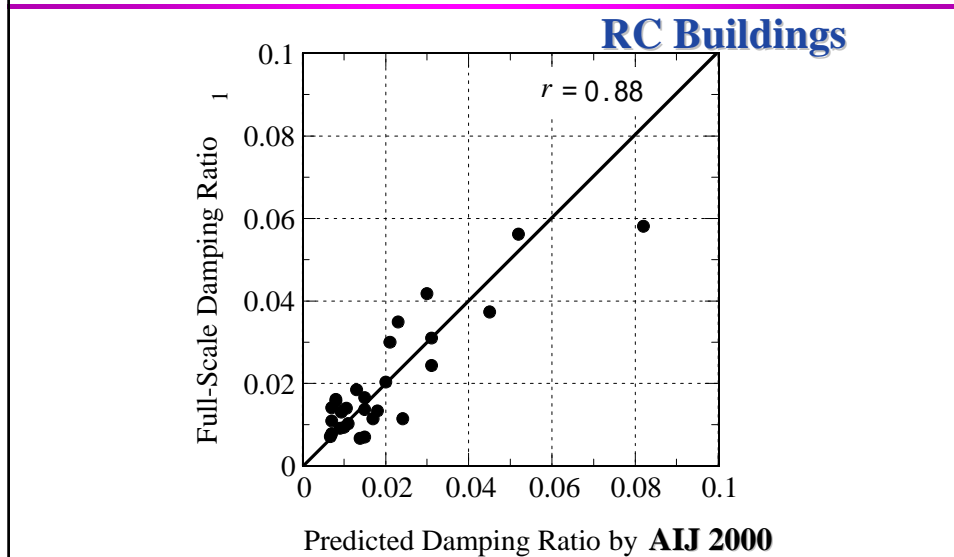
Damping Ratio
for Structural Design (AIJ, 2000)

■ **Damping Ratio for Habitability**

  - **Human Comfort**
  - **Vibration Perception Threshold**
  - *H-3 Level* (AIJ Guidelines, 1991)

■ **Damping Ratio for Structural Safety**

  - **Elastic Region**

Fundamental Natural Periods T_1 (sec)
(Damping in buildings, AIJ, 2000)

■ **RC/SRC Buildings :**
$$T_1 = 0.015\ H \quad (f_1 = 67/H)$$

■ **Steel Buildings :**
$$T_1 = 0.020\ H \quad (f_1 = 50/H)$$

■ **Ellis (1980) S/SRC/RC buildings:**
$$T_1 = 0.022\ H \quad (f_1 = 46/H)$$

H : Building Height (m)

Performance Evaluation of Habitability to Building Vibration

Guidelines for the evaluation of habitability to building vibration (AIJ, 1991)
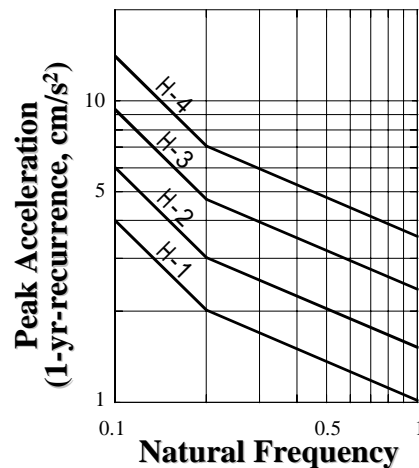
Performance Evaluation of Habitability to Building Vibration

- **1-year-recurrence Peak Acceleration**

$$A = 2.3\, f_1^{-0.431}$$

Level H-3 **: Guidelines for the evaluation of habitability to building vibration (AIJ, 1991)**
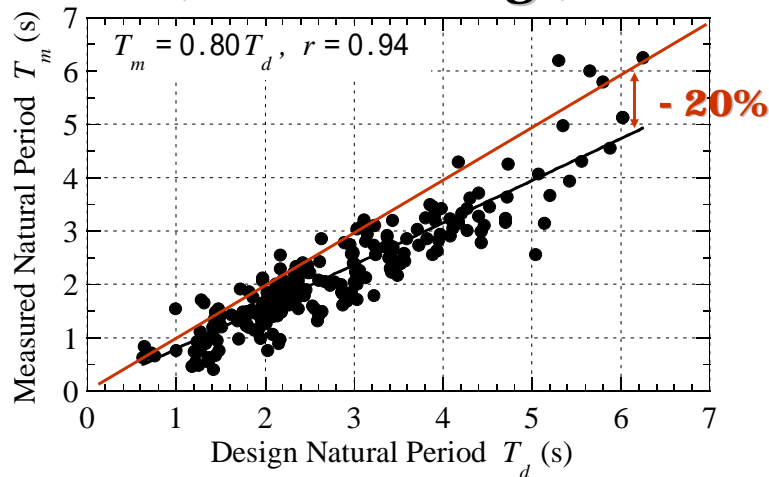
- **Foundamental natural Frequency**

$$f_1 = 1 / 0.015H \text{ (RC Buildings)}$$
$$f_1 = 1 / 0.020H \text{ (Steel Buildings)}$$

Full-scale Fundamental Natural Periods & Their Design Values

(Damping in buildings, AIJ, 2000)

(Steel Buildings)

$T_m = 0.80 T_d$, $r = 0.94$

20%

Measured Natural Period T_m (s)

Design Natural Period T_d (s)

Full-scale Natural Period $T_m^{(JDD)}$ and Design Natural Period T_d

- ## $T_m = 0.80\ T_d$

Steel Buildings : *Satake et al. (1997)*
RC Buildings : *Shioya et al. (1993)*

Contributions of Secondary Members to Stiffness

Design Damping Ratio for Structural Safety

Tip Drift Ratio $x_H/H = 2\times10^{-5}$

■ **RC Buildings**
$$f_1 = 1 / 0.018H$$

■ **Steel Buildings**
$$f_1 = 1 / 0.024H$$

AIJ 2000 (RC Buildings)

(Damping in buildings, AIJ, 2000)

Height H (m)	Habitability			Safety		
	Natural Frequency f_1 (Hz)	Damping Ratio ζ_1 (%)		Natural Frequency f_1 (Hz)	Damping Ratio ζ_1 (%)	
		Rec.	Standard		Rec.	Standard
30	2.2	2.5	3	1.9	3	3.5
40	1.7	1.5	2	1.4	2	2.5
50	1.3	1.2	1.5	1.1	2	2.5
60	1.1	1.2	1.5	0.93	1.5	2
70	0.95	0.8	1	0.79	1.5	2
80	0.83	0.8	1	0.69	1.2	1.5
90	0.74	0.8	1	0.62	1.2	1.5
100	0.67	0.8	1	0.56	1.2	1.5

- "Rec." : "Recommended" values.
- $f_1 = 1$ 0.015H (Habitability), $f_1 = 1$ 0.018H (Safety)
- Safety : Elastic Range

AIJ 2000 (Steel Buildings)

(Damping in buildings, AIJ, 2000)

Height H (m)	Habitability			Safety		
	Natural Frequency f_1 (Hz)	Damping Ratio ζ_1 (%)		Natural Frequency f_1 (Hz)	Damping Ratio ζ_1 (%)	
		Rec.	Standard		Rec.	Standard
30	1.7	1.8	2.5	1.4	2	3
40	1.3	1.5	2	1.0	1.8	2.5
50	1.0	1	1.5	0.83	1.5	2
60	0.83	1	1.5	0.69	1.5	2
70	0.71	0.7	1	0.60	1.5	2
80	0.63	0.7	1	0.52	1	1.5
90	0.56	0.7	1	0.46	1	1.5
100	0.50	0.7	1	0.42	1	1.5
150	0.33	0.7	1	0.28	1	1.5
200	0.25	0.7	1	0.21	1	1.5

- "Rec." : "Recommended" values.
- $f_1 = 1$ 0.020H (Habitability), $f_1 = 1$ 0.024H (Safety)
- Safety : Elastic Range

Effects of Building Use

(Damping in buildings, AIJ, 2000)

Steel Buildings

- **Office Buildings**

  $\zeta_{AVE} = 1.15$ % ($H_{AVE} = 112.6$m)

- **Hotels and Residential Buildings**

  $\zeta_{AVE} = 1.45$ % ($H_{AVE} = 100.4$m)

25% Increase due to interior walls

Ratio of Higher Mode Damping to Next Lower Mode Damping
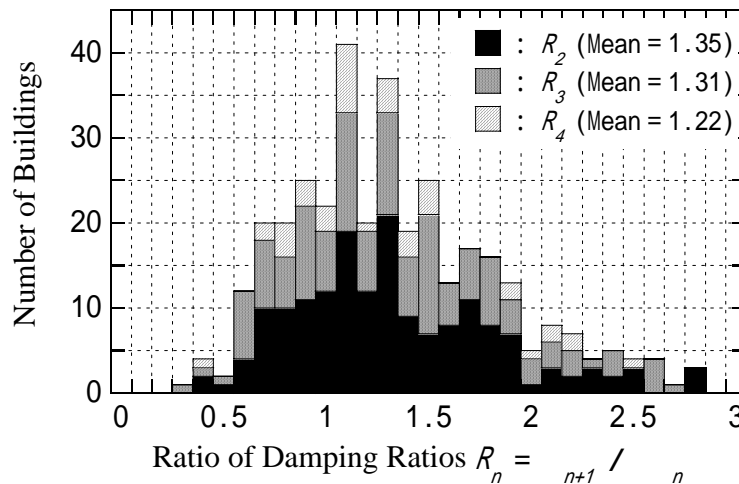
Steel Buildings
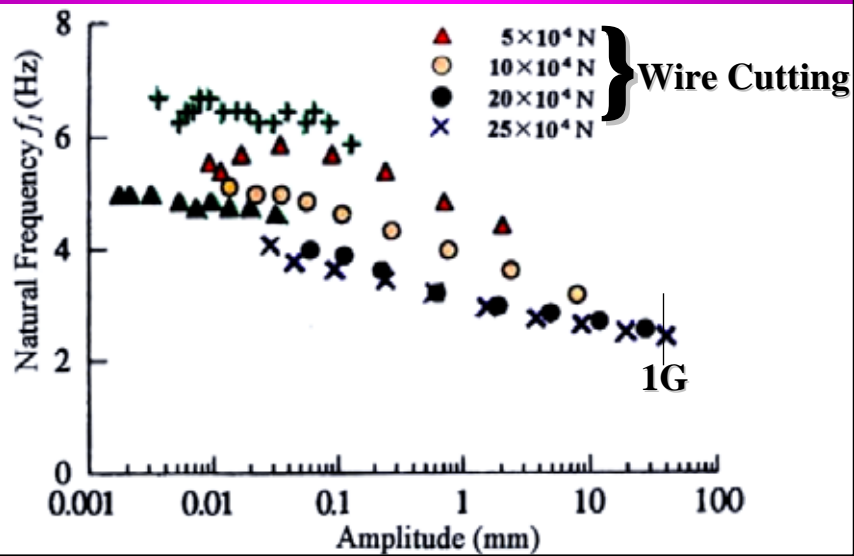

Higher Mode Damping Ratio

(AIJ2000)

- **RC Buildings**

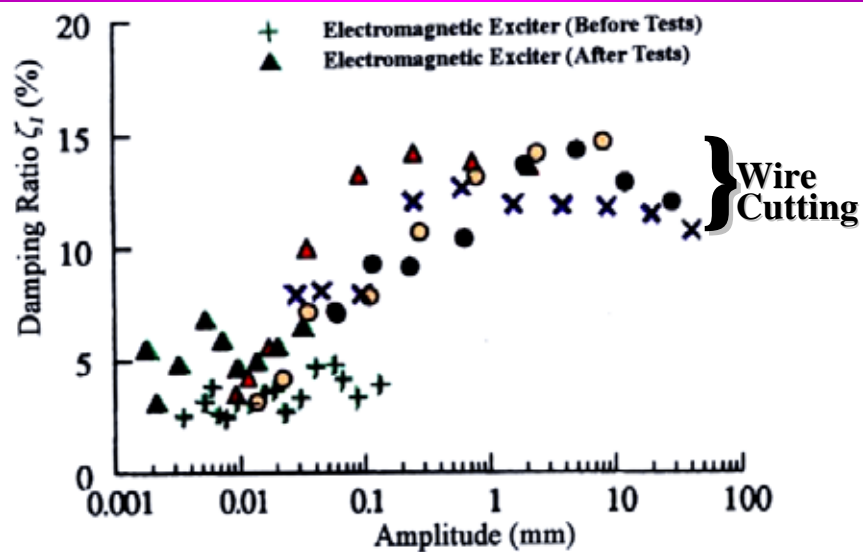$$\zeta_{n+1} = 1.4 \, \zeta_n \, , \quad (n=1,2)$$

- **Steel Buildings**

$$\zeta_{n+1} = 1.3 \, \zeta_n \, , \quad (n=1,2)$$

Large Amplitude Tests
(A Steel Model House)

Large Amplitude Tests
(A Steel Model House)

Damping Ratio
for Ultimate Limit State

- Damage to Secondary Members
- Development of Micro Cracks

↙**Larger Damping Values**

   Almost No Quantitative Evidence

■**Effects of Hysteretic Response of Frames**

Evaluation of Damping Ratio from
Randomly Excited Motion

Output Information
    Spectral Methods
     Hal-Power Method
     Auto-Correlation Method
      Stationarity is strictly required.
    Random Decrement Technique
     Stationarity is not necessarily required.
     Appropriate for amplitude dependent phenomena
     Each mode should be clearly separated.
    Frequency Domain Decomposition
     Each mode does not have to be well separated.

35-03

37

Random Decrement Technique
Estimation by SDOF Fitting

$x(t)$

x_0

0

t
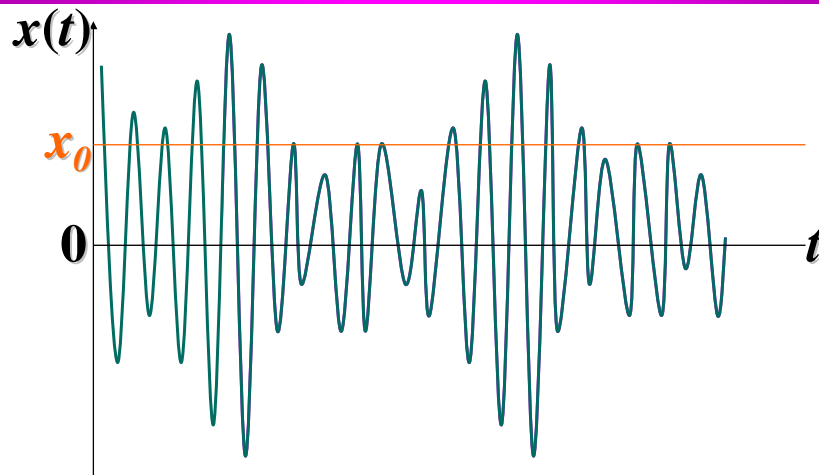
35-04

Random Decrement Technique
Estimation by SDOF Fitting

$x(t)$

v_0

x_0

0

t

Sub-sample
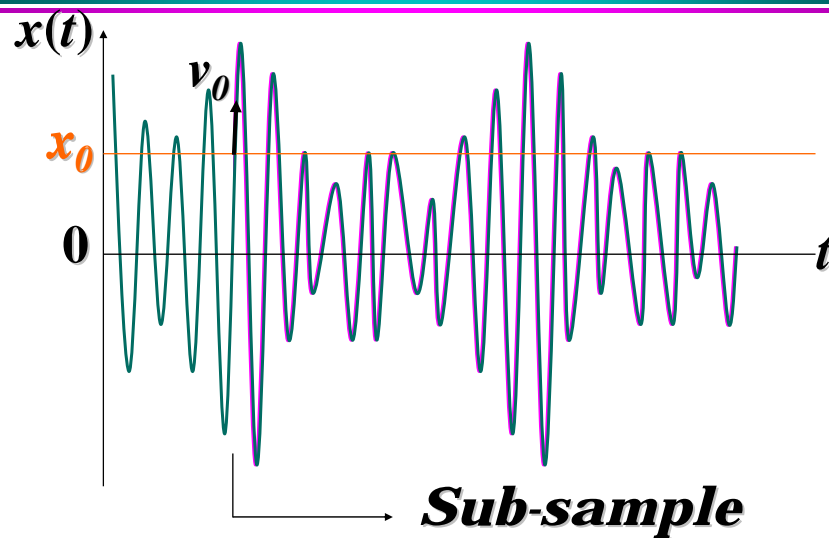
35-05

Random Decrement Technique
Estimation by SDOF Fitting

$x(t)$

x_0

v_0

0

t

Sub-sample

35-06
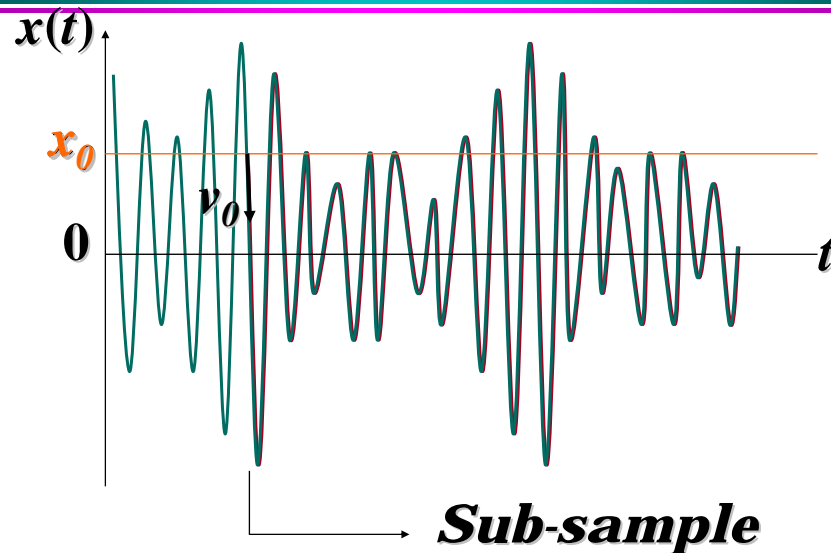
Random Decrement Technique
Estimation by SDOF Fitting

General Solution of SDOF

$$M\ddot{x} + C\dot{x} + Kx = f(t)$$

zero-mean random excitation

$$x(t) = D(t) + R(t)$$

$D(t)$: **Damped Free Component Depending on Initial Condition** (x_0, v_0)

$R(t)$: **Randomly Excited Component**

$$= \int_0^t f(\tau)h(t-\tau)d\tau$$

Superimposition of Sub-samples (Ensemble Averaging)

35-07

39

Random Decrement Technique
Estimation by SDOF Fitting

Superimposition of Sub-samples (Ensemble Averaging)

= **Random Decrement Signature**

$\propto$ **Auto-correlation Function**

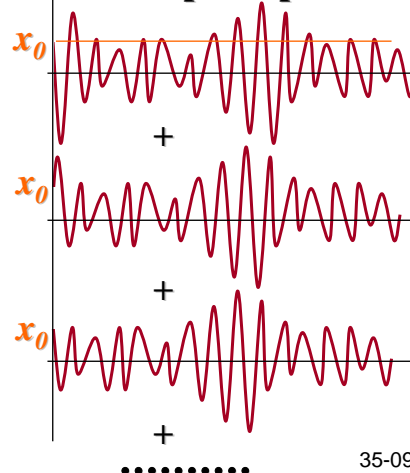$\approx$ **Damped Free Component with Initial Amplitude x_0**

$$\propto \exp(-\zeta\omega_0\tau)(\cos\sqrt{1-\zeta^2}\,\omega_0\tau + \frac{\zeta}{\sqrt{1-\zeta^2}}\sin\sqrt{1-\zeta^2}\,\omega_0\tau)$$
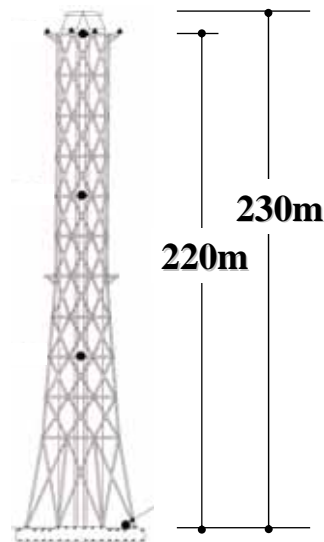
35-08

Random Decrement Signature

35-09

40
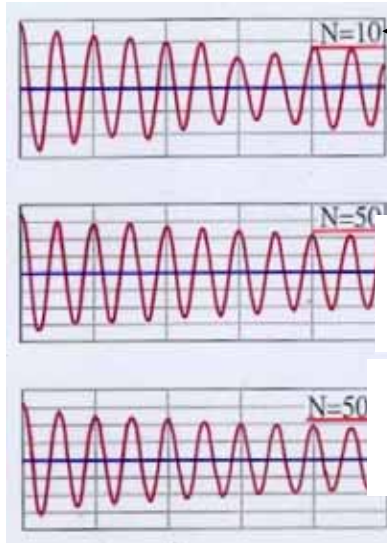
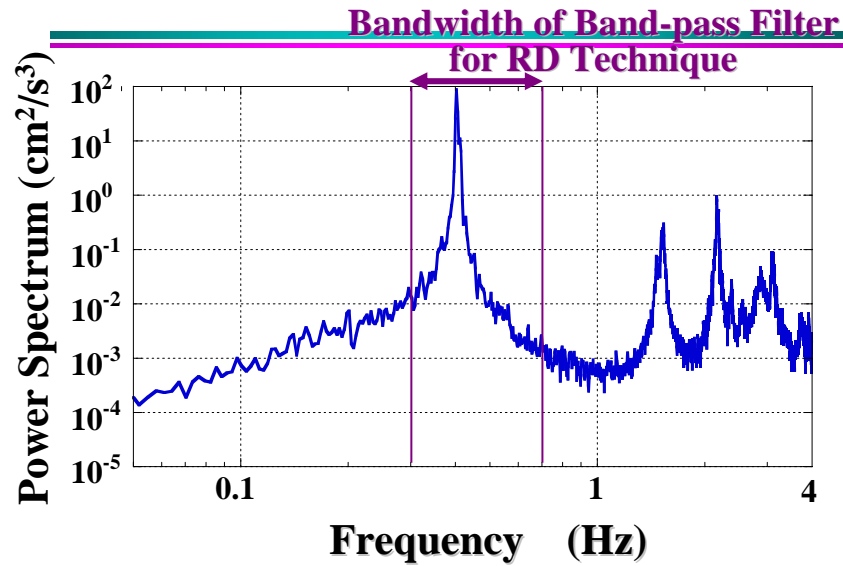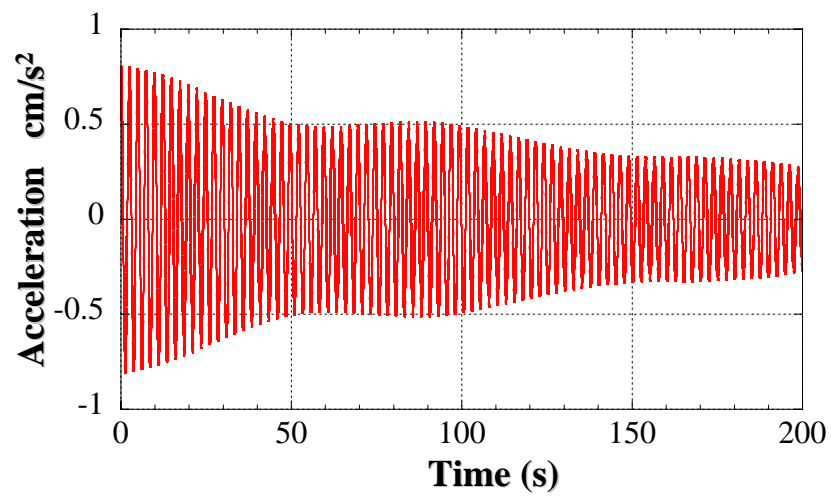**Damping Estimation of Chimney with Closely Located Natural Frequencies by Random Decrement Technique**

230m

220m

35-10

Power Spectral Density of Ambient Acceleration Response (NS comp. at 220m)
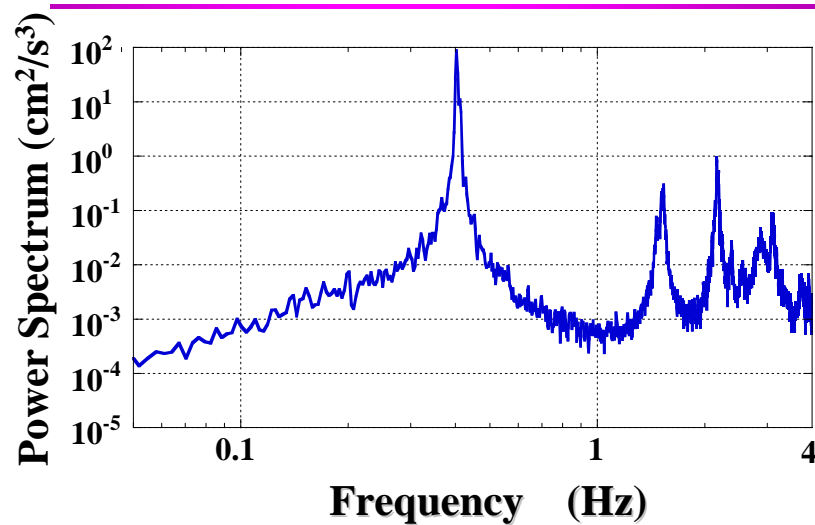
Power Spectrum (cm²/s³)

10^2
10^1
10^0
10^{-1}
10^{-2}
10^{-3}
10^{-4}
10^{-5}

0.1   1   4

Frequency   (Hz)

Power Spectral Density of Ambient Acceleration Response (NS comp. at 220m)

Bandwidth of Band-pass Filter for RD Technique

Power Spectrum (cm²/s³) vs Frequency (Hz)

Random Decrement Signature

Acceleration cm/s² vs Time (s)

Power Spectral Density of Ambient Acceleration Response (NS comp. at 220m)

0.40Hz
0.41Hz

Power Spectrum (cm²/s³)

Bandwidth of Low-pass Filter

Frequency (Hz)
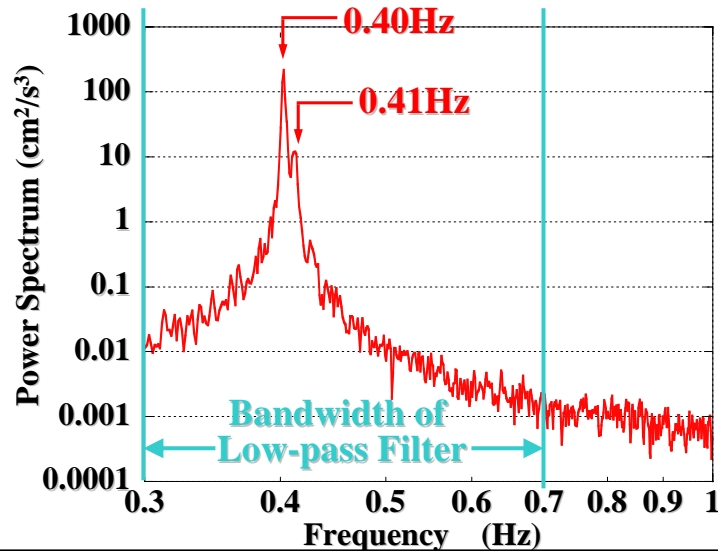
35-11

Least Square Approximation of MDOF Random Decrement Signature

$$x_1 = \frac{x_{01}}{\sqrt{1-\zeta_1^2}} \, e^{-\zeta_1\omega_1 t} \cos\left(\sqrt{1-\zeta_1^2}\,\omega_1 t - \phi_1\right)$$

$$+$$

$$x_2 = \frac{x_{02}}{\sqrt{1-\zeta_2^2}} \, e^{-\zeta_2\omega_2 t} \cos\left(\sqrt{1-\zeta_2^2}\,\omega_2 t - \phi_2\right)$$
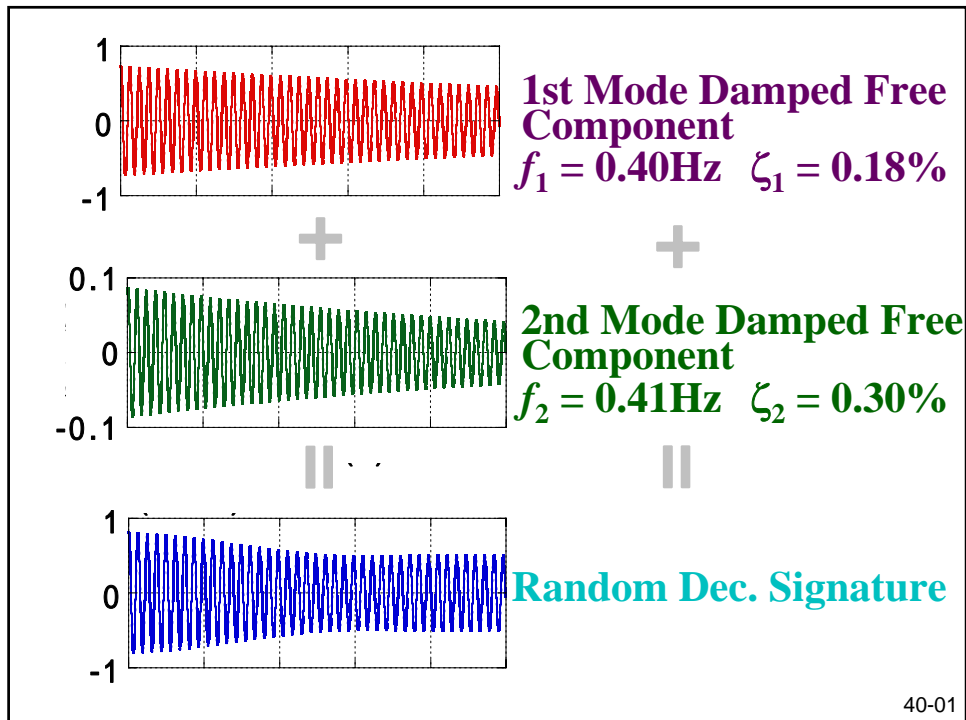
$$+$$

$$+$$

$$x_N = \frac{x_{0N}}{\sqrt{1-\zeta_N^2}} \, e^{-\zeta_N\omega_N t} \cos\left(\sqrt{1-\zeta_N^2}\,\omega_N t - \phi_N\right)$$
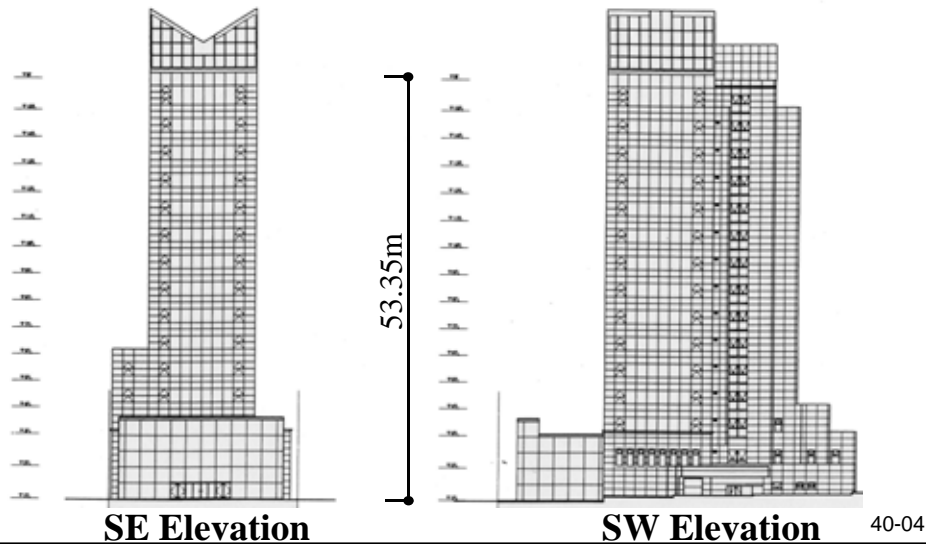
Mean Value Error

$$x = x_1 + x_2 + \quad + x_N + m$$

35

43

1st Mode Damped Free Component
$f_1 = 0.40\text{Hz}$ $\zeta_1 = 0.18\%$

2nd Mode Damped Free Component
$f_2 = 0.41\text{Hz}$ $\zeta_2 = 0.30\%$
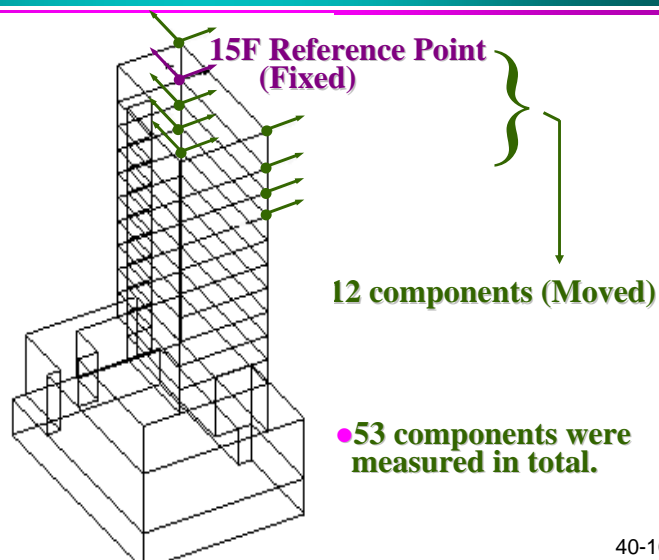
Random Dec. Signature

40-01

Estimated Dynamic Characteristics of a 230m-high Chimney by 2DOF RD technique and FDD

Mode #	Natural Frequency (Hz)		Damping Ratio (%)	
	RD	FDD	RD	FDD
1	0.40	0.40	0.18	0.24
2	0.41	0.41	0.30	0.39
3	1.47	1.47	0.83	0.30
4	1.53	1.52	0.85	0.91
5	2.17	2.17	0.55	0.65
6	2.38	2.38	0.42	0.39
7	–	2.87	–	–
8	–	3.10	–	0.77

40-02

Full-scale Measurement of Dynamic Properties of a 15-story CFT Building

53.35m

SE Elevation   SW Elevation   40-04

Ambient Vibration Measurement of Completed Building

15F Reference Point (Fixed)

12 components (Moved)

● 53 components were measured in total.

40-10

Frequency Domain Decomposition (FDD)

Spectral Density Matrix of Measured Responses

$G_{yy}(j\omega)$

Singular Value Decomposition

$$G_{yy}(j\omega_k) = U_k S_k V_k^H$$

- **Singular Value ($\omega_k \approx \omega_i$) becomes large**
  $\rightarrow$ **has a peak equivalent to SDOF-PSD function**
- **Left Singular Vector u_r associated with a peak**
  $\approx$ **Mode Shape**

Natural Frequencies, Damping Ratios, Mode Shapes

FDD : Basic Formulations

- **PSD: Input/Output relation**

$$G_{yy}(j\omega) = H(j\omega)^* G_{xx}(j\omega) H(j\omega)^T$$

- **PSD: Modal Decomposition**

$$G_{yy}(j\omega) = \sum_{r=1}^{N} \frac{d_r \phi_r \phi_r^H}{j\omega - \lambda_r} + \frac{d_r \phi_r \phi_r^H}{j\omega - \lambda_r^*}$$
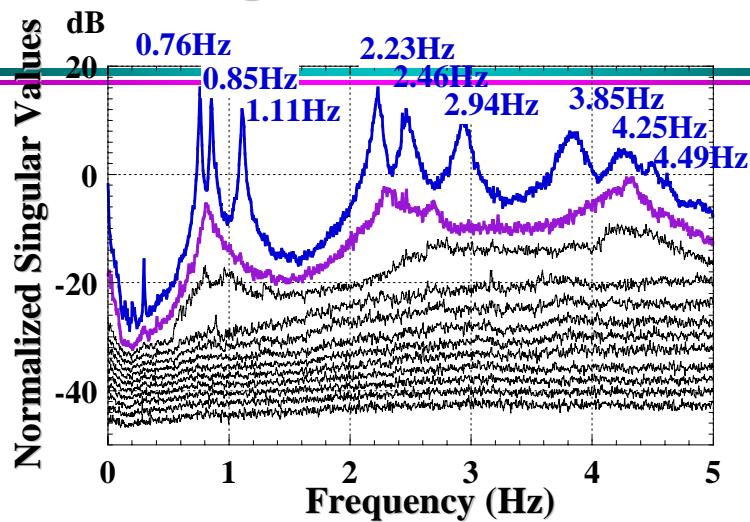
- **PSD: Singular Value Decomposition**

$$G_{yy}(j\omega_k) = U_k S_k V_k^H$$

- **Mode Shape Estimation**

$$\hat{\phi}_r = u_r$$

Singular Value Plots

0.76Hz
0.85Hz
1.11Hz
2.23Hz
2.46Hz
2.94Hz
3.85Hz
4.25Hz
4.49Hz

Normalized Singular Values

dB

Frequency (Hz)

• Peak-Picking
• Average of Normalized S.V. of PSD Matrices of All Data Sets
• Analytical Software: ARTeMIS

40-13

Identification of Closely Located Peaks
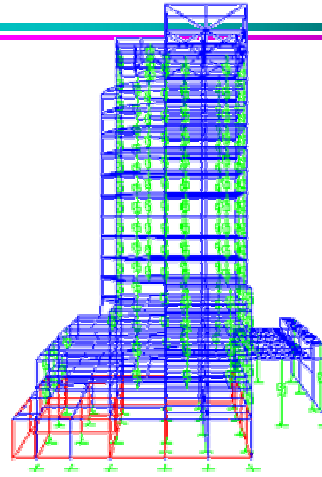## - SV Plot : Single Mode Selection -

1st Mode
Component

2nd Mode
Component

0.76Hz

0.85Hz

40

47
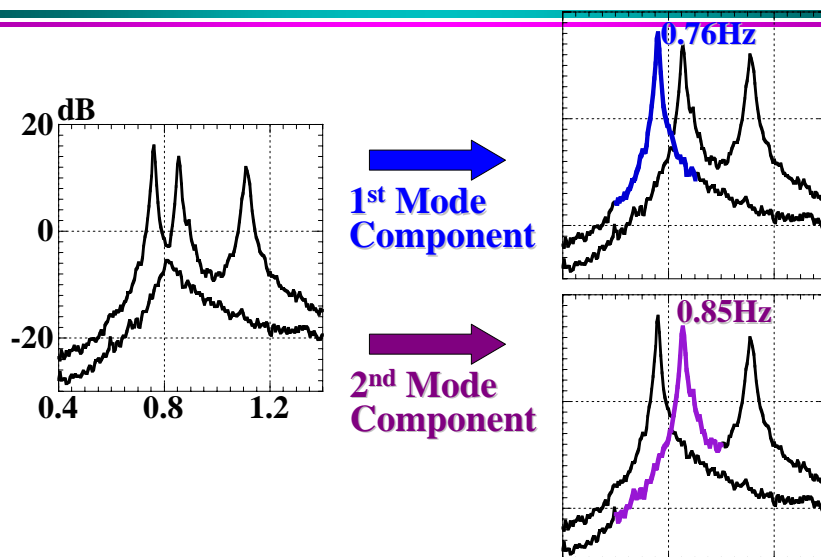
FEM Analytical Models
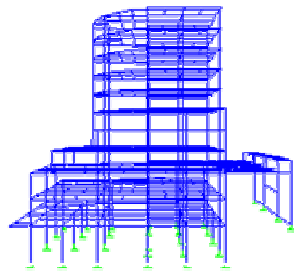
11-story Model   15-story Model

45-01

Natural Frequencies of 15-Story CFT Building *Field Data*

Mode	FEM (Hz)	AMB (Hz)	Error (%)
1	0.76	0.76	0
2	0.87	0.86	2.22
3 *Adjusted by Additional*	1.15	1.11	3.51
4 *Stiffness*	2.14	2.23	-3.99
5	2.53	2.47	2.59
6	3.02	2.94	2.82
7	3.85	3.85	0
8	4.26	4.26	0
9	4.67	4.47	4.29

45-02

FDD IDENTIFIED MODE SHAPES (1-3)

$f_1 = 0.760$ Hz $f_2 = 0.854$ Hz $f_3 = 1.111$ Hz
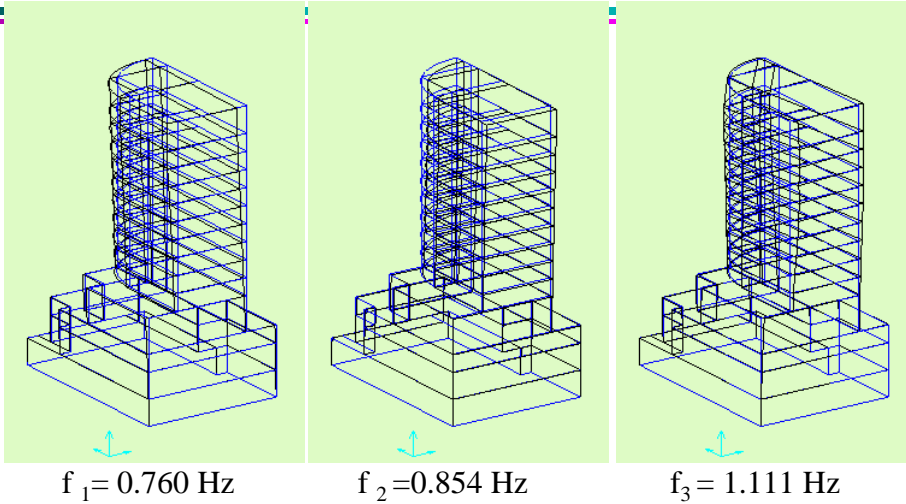
45-03

FDD IDENTIFIED MODE SHAPES (4-6)

$f_4 = 2.230$ Hz $f_5 = 2.468$ Hz $f_6 = 2.939$ Hz

45-04

49

FDD IDENTIFIED MODE SHAPES (7-9)

f$_7$= 3.849 Hz   f$_8$= 4.255 Hz   f$_9$= 4.493 Hz

45-05

Mode Shapes by FDD & FEM

y

x

1st Mode (*y* dir.)

2nd Mode (*x* dir.) 45-06

50

Mode Shapes by FDD & FEM

4th Mode (*y* dir.)   5th Mode (*x* dir.) 45-07

Mode Shapes by FDD & FEM

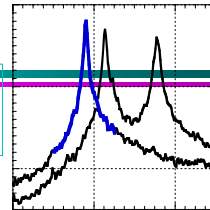7th Mode (*y* dir.)   8th Mode (*x* dir.) 45-08
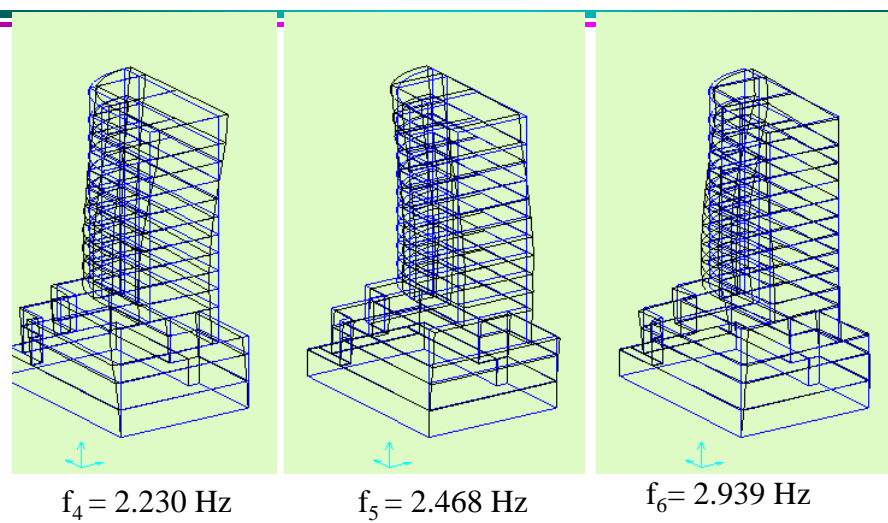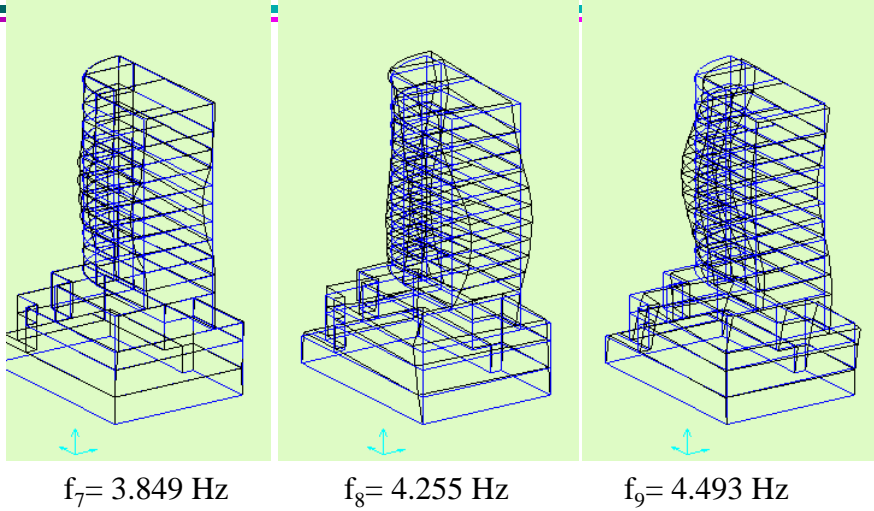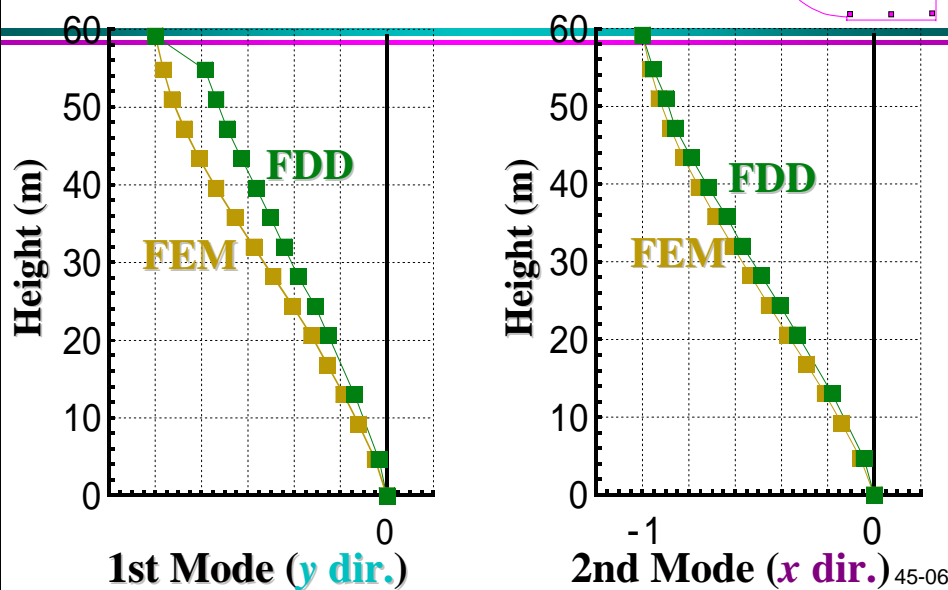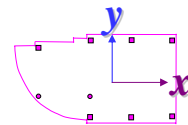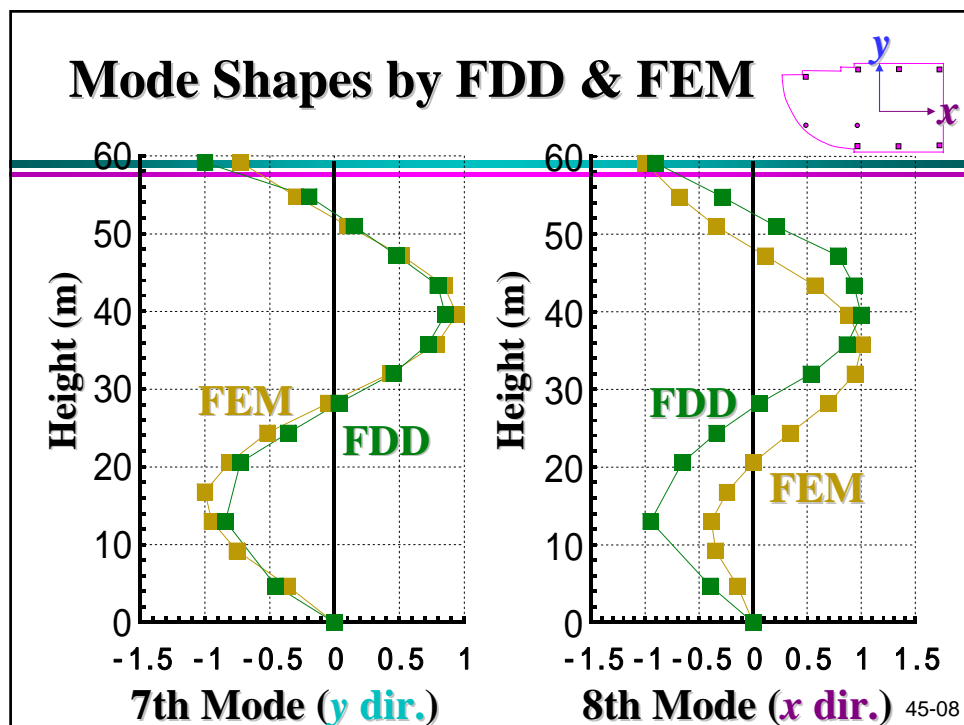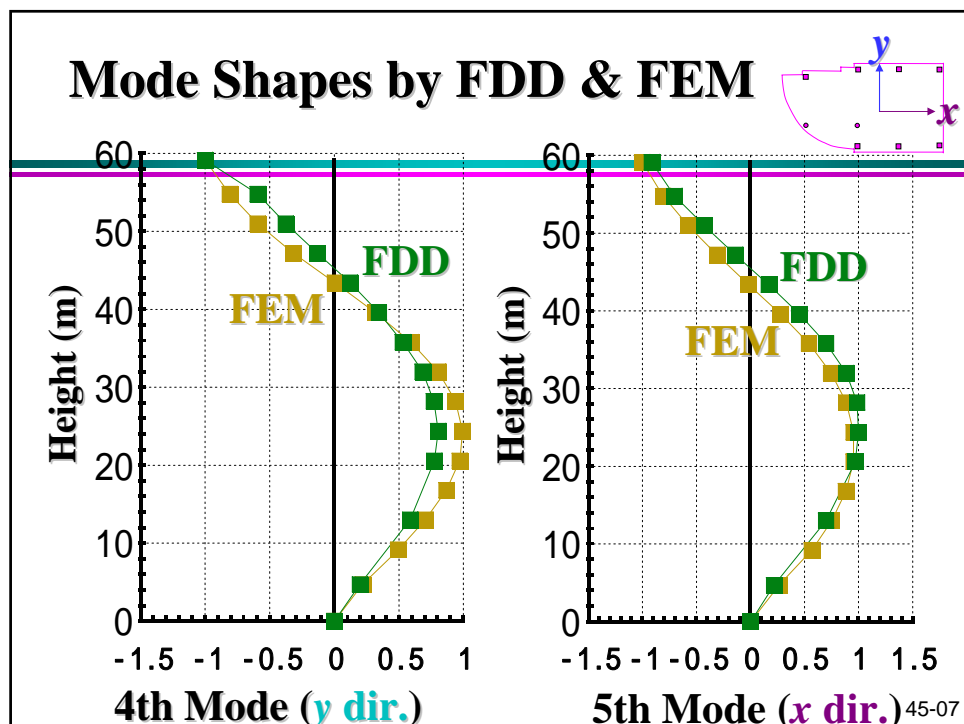
Basic Idea & Procedure of Damping Estimation

■ **Select SDOF approximation of the "PSD Bell" based on using MAC**

■ **Calculate SDOF correlation function via Inverse FFT of the selected "PSD Bell"**

■ **Estimate damping ration by Logarithmic Decrement Technique**

45-09

Damping Estimation

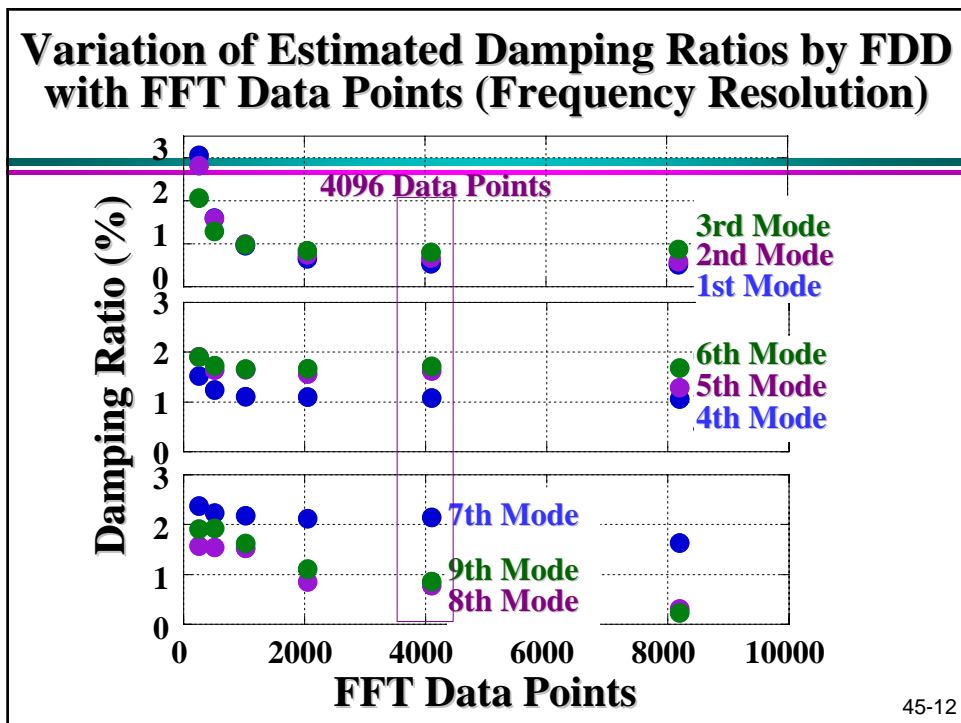**Inverse Fourier Transform of Identified Mode Component (SDOF-PSD)**

Auto-Correlation Function: $R(\quad)$

1st Mode

$\dfrac{R(\quad)}{R(0)}$

f_1=0.76Hz, ζ_1=0.54%

45-10

52

Variation of Estimated Damping Ratios by FDD with FFT Data Points (Frequency Resolution)

45-11

Variation of Estimated Damping Ratios by FDD with FFT Data Points (Frequency Resolution)

45-12

53
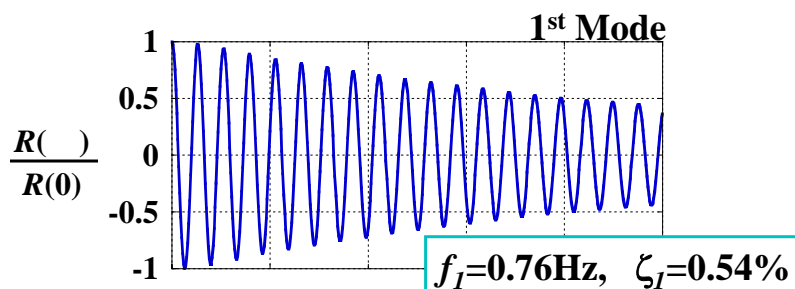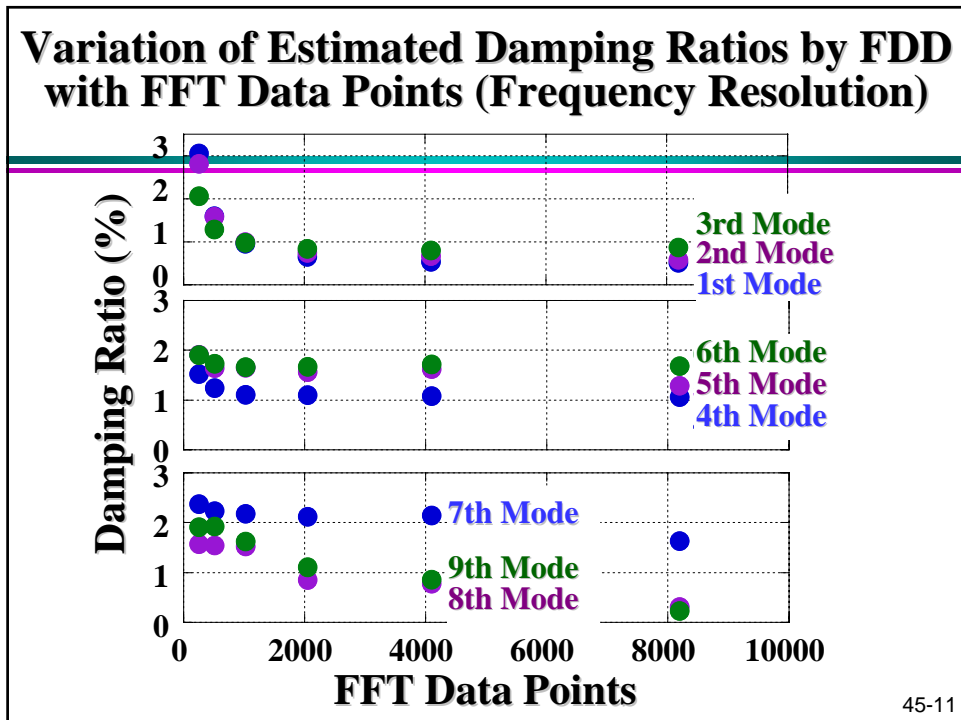
Estimated Damping Ratios and FFT Data Points

Data Points	256	512	1024	2048	4096	8192
1st	3.05	1.60	0.95	0.65	0.54	0.51
2nd	2.81	1.58	0.99	0.74	0.67	0.58
3rd	2.06	1.29	0.98	0.84	0.80	0.87
4th	1.52	1.24	1.11	1.10	1.08	1.06
5th	1.91	1.64	1.65	1.56	1.62	1.29
6th	1.90	1.73	1.66	1.67	1.72	1.68
7th	2.37	2.23	2.18	2.15	2.11	1.63
8th	1.57	1.60	1.38	0.85	0.78	n/a
9th	1.91	1.92	1.62	1.25	0.86	n/a

45
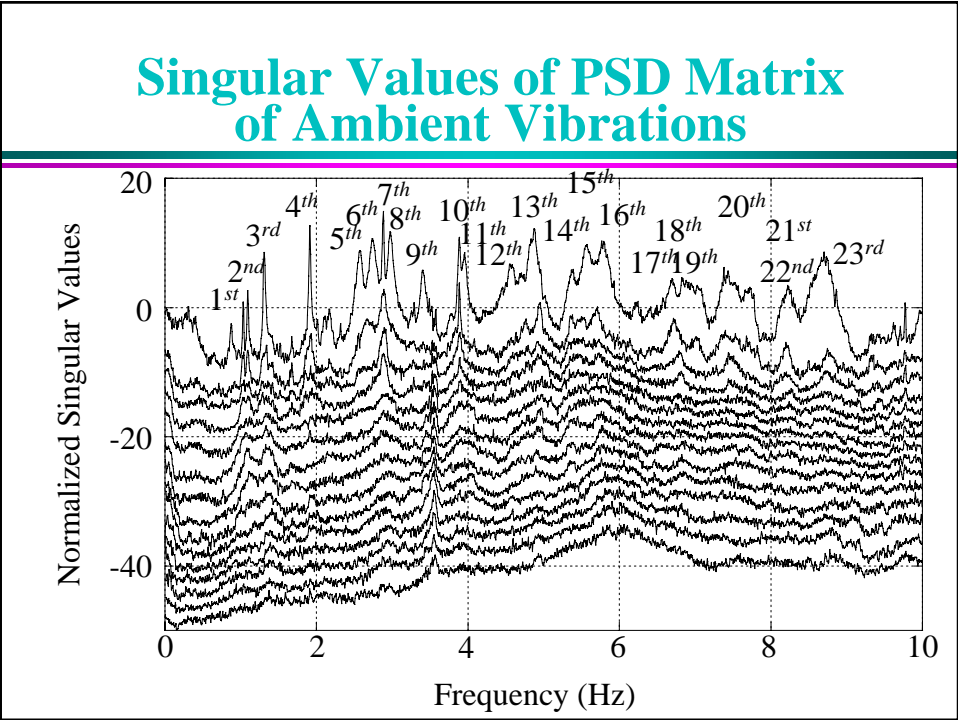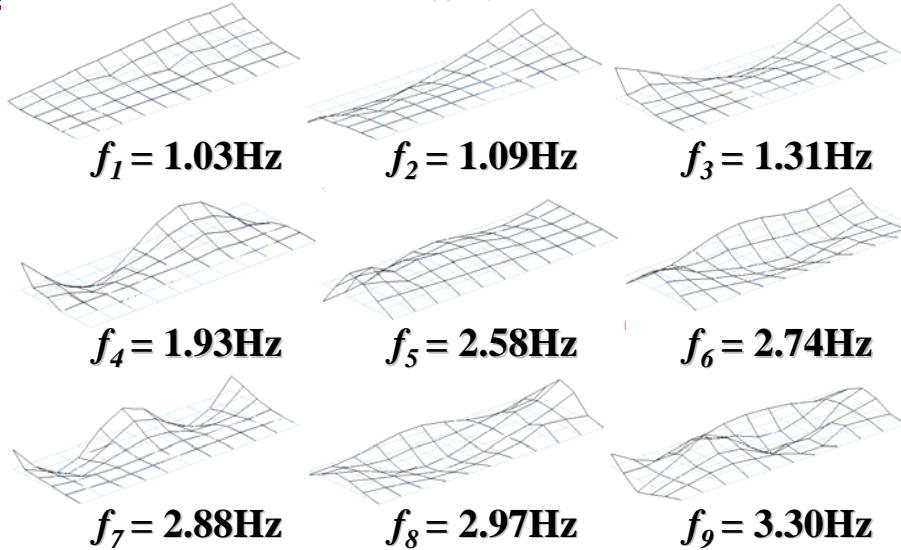
Singular Values of PSD Matrix of Ambient Vibrations

45

54

Mode Shapes Obtained by
SVD of PSD Matrix

$f_1 = 1.03\text{Hz}$ $f_2 = 1.09\text{Hz}$ $f_3 = 1.31\text{Hz}$

$f_4 = 1.93\text{Hz}$ $f_5 = 2.58\text{Hz}$ $f_6 = 2.74\text{Hz}$

$f_7 = 2.88\text{Hz}$ $f_8 = 2.97\text{Hz}$ $f_9 = 3.30\text{Hz}$

Mode Shapes Obtained by
SVD of PSD Matrix

$f_{10} = 3.90\text{Hz}$ $f_{11} = 3.94\text{Hz}$ $f_{12} = 4.58\text{Hz}$

$f_{13} = 4.86\text{Hz}$ $f_{14} = 5.38\text{Hz}$ $f_{15} = 5.57\text{Hz}$

$f_{16} = 5.79\text{Hz}$ $f_{17} = 6.70\text{Hz}$ $f_{18} = 6.83\text{Hz}$

Mode Shapes Obtained by SVD of PSD Matrix

$f_{19} = 7.00\text{Hz}$ $f_{20} = 7.42\text{Hz}$ $f_{21} = 7.71\text{Hz}$

$f_{22} = 8.23\text{Hz}$ $f_{23} = 8.70\text{Hz}$
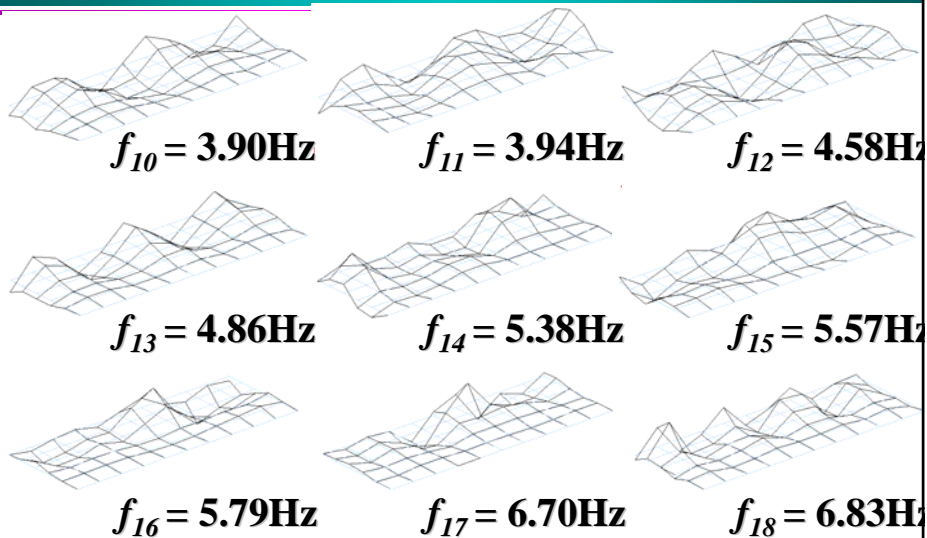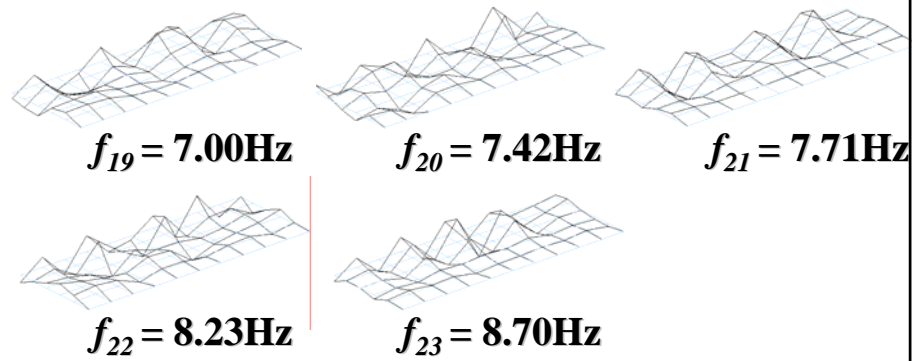
Damping Ratios Obtained by SVD of PSD Matrix

Mode	ζ (%)	Mode	ζ (%)	Mode	ζ (%)
1	0.69	9	0.91	17	0.73
2	0.59	10	1.44	18	0.75
3	0.56	11	0.66	19	0.50
4	0.21	12	0.98	20	0.51
5	2.17	13	1.01	21	1.04
6	1.38	14	0.83	22	0.72
7	1.47	15	0.85	23	0.50
8	0.27	16	0.61	-	-